Study Material On Strength of Material

Department of Mechanical Engineering



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(Affiliated to Biju Patnaik University of Technology, Odisha and SCTE & VT, Odisha, Approved by AICTE, New Delhi and Recognised by Govt. of Odisha)

external combined effect of defined as the A 1000 may be acting on a body

(1) loads can be classified as

Live on Huckeathy load → Dead local

Inentia load

centritegal 100d

d can be clanified

1 Trapile 1000

comprensive 100d

Porsional on twinting load

1000 Bending

load

of road occording to pl. of application Bulmarys elar, sitication Another

point load or concentrated toads

It is concentrated at a single pt

pection. d Lilility CHOND P Unisbamly diplaibeled tood It in diplaibeled and a Dishabuted tood

pool Burguon Plumoping to

when a body acted up on by nome toad it undergoes deformation The enternal resembonce objered by the body to meet with mall of body it i.e change in abape and pize object increases gradually. Des deformation, the material of the body resin the tendency of the load to deferm the body, and when the load enflerence taken over by the enternal nesembonce of the becomes stable. States :-

load to called which ".

1

Cishte. sheen. (a) Unit 4ir Total considered eilber Stren can be

aesiplance to an external effect EN N, KARMA expressed It co ity Tolal chan! It in the total called total others.

3.0

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R

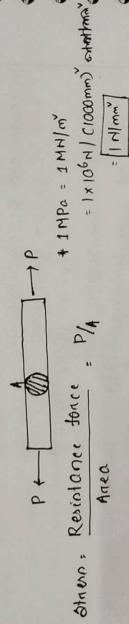
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A 7 1 1

Also

er und staenor

tour-The aestistance developed per unit area in called en expressed en Almm", MMIM's KAIM". staeso. It



Types of phenon.

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(e) Abean lay Tennion lby compaennion if dimple on dinect nhan

@ Indinect other

cas Bending (b) Twenting

(4) combination of type -1 & type - 2.

(0) Tennile shanos

The normal phasm which cause extension on the member in called tensile phasm. Here the applied force in pell. The force in acting perpendicular to the deformation plane.

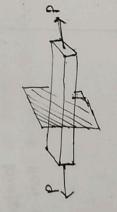
(b) compressive stress!

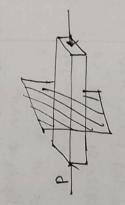
perpendicular commercial atrien. Here the applied tome The normal natures which counces compression on the member in ealled acting in to the deformation plane. peop. The force

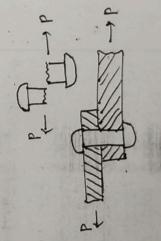
called as normal ofner plane. 3 * Both tennile 2 compressive nationes as force in perpendicular to deformation

(c) show natural.

The connesponding The toace which in acting povalled deformation member en in called obton force. in the enonnection of object daen. developed प्रम् ealled







9.0

Strain:

deformation steel, cost inan, brass, conenete, in no amall that it cannot be visible to naxed eye. Extennemeter, bano extend at temple load electain strain gauge are the instruments are used to measure the None of the materials are perfectly aigid. As we know when tonce etc. undergoes deformation when torce applied on it. But the extension. The experiments shown that the aborten under compressive load. applied on rebber it extends. demilaly

stacks in detend as change in dimension to original dimension, two types of ninain onlines depreases as total volume of the material in name and the vice-vena length indeases the enous section so concept of tennile load as the occoun at compression load. Burnp

लाह. #DOU'S

AA 412 onigenal enonnection change in monorection Chonge in length Oreignal tength Lateral phrain (ea) where whain

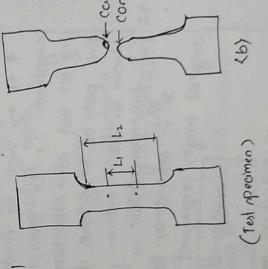
Shen- Shain Relation?

ong material in obtained by ecnducte behave differently under opeaimen. Different matt. nelation of tennile test on ntanded The streen- stacky

tennion and compression.

Behavious on Tennion & Mild Aleel appeainent!

coivenal at eth both endn. at negular entervaln. Atter certain load gradually increased till the opening in applied gradually at the endor and a typical mild extendion measured extension in eleases at tooler note. Load gouge length (4). Load Extennomety in titled to meaner the gaipped at Buf w testing machinic cutm) ateel test openimen age 1000 and the Ove nwocho extendion An



Load dirided by augmal enonnectional in them what in obtained in called as nominal places or nemply places. Alacin in obtained and reten in 4-axis. The googe lengthat). A graph extendometer neading with dividing extensioneter neading with parepared by taxing stain in x-axin batecks cAn obown in Hig-b)

0.6

2

1

1-6

17 1 0

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3 2 3 F P P plann at which tenally the openimen fails in called breaking loadied atter elastic times a permenul a straight A19-C * If the math in unloaded within elastic times the angunal length in It in the point at which the load plants neducing and the externies and the nations points on At thin point the naturn remains name and the strain engenes Sylca B trial extension at acapture to phase the math can never 41 the olage 1 = ourginal length Original Anea. 4.3 percentage Reduction in allegite of maximum abange in enon predional A1= Fernal Anea 1's Final length Strain it tellown of material. genre tollown the name path nevernely atten the elastic umit it enloaded 001 × 7-7 ×100 en esteament the phanomenon in called yielding as placen places diagram Stamon in destined as the natio of the A A expressed, as percentange. the others in naid to be dirappeared up to which est the load en nemored up to which othern in directly propapize and Flongation = Reduction = It in the temiting value of other It is the limiting value of strem path of FF'. Thun is it in enonn-ne elecnal > (a) Limit of proportionality (11)? ortho of the aegains to the original This is the maximum percentage - upper yield point (B): percentage - Lower yield point (C): + Ultimote olders (D)? percentage Elongation? - Baroaring point (E): Elastic umit and: - ntional to phosin. negained. ize the graph are > original called for nome teme. neck toamation of now in left. oniginal lengths enonpreeteenal भिष्ठ (१) विस graph in 14 古 もも · twood ENE

4.4 Behaviour of material under compression:

An there in a chance of backing (laterally bending) of long specimen, ton compression test about apecimena one ened thin test involves measurement of smaller changes in length.

of In case of ductile material stress strain cours tollows exactly some path an in tennile test up to and even alightly beyond yield point. For larger values of curre direiger. In this case there will be no

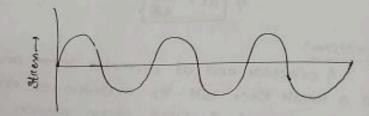
neck tomation.

-> For most brittle materials alternate compressive places in compression in much larger than in tennion. It in because of flows and eraces present in brittle materials which weaken the mattern tennion bed will not affect the plangth in compression.

Behaviour of malerial under appealed toadings:

when a material in publicled to nevernal at other that in from tenpile to compressive and compressive to tennile then it in paid to be repeated loaded. This type of vorging streets affect the strength of material and this effect in called tateque

31. Short loaded with pulley notating at a particular RPM.



6. Factor of safety:

In real practice it is not possible to design a member permitting up to ultimate stress due to tollowing reasons. -> Reliability of mall may not 100x due to metallergical detect

-> Loado taxen by the designer one only estimated toods.

- occanionally come members may be avuloaded.

- some ideal conditions are assumed during design.

do, the maximum othern to which any member in designed in

much less than the attemate street and in called working street. The notio of ultimate othern to working othern in called an

toctor of notety.

factor of notety : working street

The value of tactor of nately too name matt are

Steel - 1.85

concrete - 3

Tember - 4 to b

House's Lun:

Robert Hooke, an english mathematician conducted neveral experiments and condluded that,

"alaem in directly proportional to almain with in elastic limit." Thin in called an Hooken low.

Hence a = Ee

Here, E is the constant of proportionality and known as modules as elasticity or young's modules.

NOW, Stresn(a) = F/A atran (e)= AL/L

According to Hocke'n law

$$a: Ea \Rightarrow E: \frac{a}{a} = \frac{F/A}{AI/L} = \frac{FL}{A.AL}$$

$$\Rightarrow AL = \frac{FL}{AE}$$

problem !-

A cincular nod of diameter 20mm and 500 mm long in newspected to a tennile torce 45%. The modules at elasticity ton affect may be taken as accountment. Find stress, strain and elongation at the bar due to applied load.

given data,

load (F) : 45 A : 45000 A

Diamet u (d) = 20 mm => Acea = 7/4 d = 7/4 x (20) = 314.159 mm

Length (1) = 500 mm

young's modellers (E) + 200xN)mm : 200 x103 N/mm

$$\rightarrow 84\pi \, cun \, (e) = \frac{\Delta t}{c} = \frac{0.358}{500} = \frac{0.000716}{1600}$$

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. 3

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problem !-

Following data never to a mild steel operamen tested in a

laboratory.

- Dromeles of the opecimen - asmm

- -> Length of the operation: 300 mm
- Load at yield point : 127.65KN
- Maximum load : 208.60 KM
- Length of opecimen often tailcre = 375mm
- Neck diameter = 17.75mm

Determine (a) young's modules (b) yield stress (c) ultimate stress (d) x.ag. at elongation (e) x. ag. at neduction (t) sate ntnews adopting

"Breek to the light separation that it is a second to the

many the many control of the first of the fi

a FOS : 2.

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problem!

A hollow steel tube in to be used to compa an oxial compressive tood of 190 km. The gread alread of ofeel in 250 Mmm. A tactor of nately of 1-15 in used in the design. The tollowing three classes of terben of external diameter 101.6 mm are orailable.

light = 3.65 mm, Medium = 4.05 mm, Heavy = 4.85 mm (Horagness) which nection do you recommend?

by yield stress (oy) = 250 Hlmm

Factor of natety = 1.75

80, perminpible phreso : 04 : 250/175 : 142.857 Mmn

Load (F) = 140 KM = 140 × 103 M.

Streen (a) = F/A => 142.857 = 140×103

=> A = 140×103 = 980 mm

oue of pfeel tube = 7/4 (Do - Di) = 980 [Do: July diamety We KNOW

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do

220000

=> Ty [101.6) - a] = 986

=> d" = 9074 . 784 => d = 95.262 mm

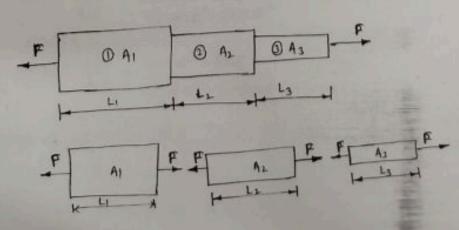
through en (+) = D-d = 101.6 - 95.262 : 3.169 mm.

Hence, use of tight nection in recommended.

Born with ranging cronnection:

A box with exans- sections varying in steps and subjected to axial load in as abown in fig. Let the lengths be 11,121, and the errorn nection be A1, A, 1A, respectively. 'E' be the young'n modellus the and "p' in the arrial load applied.

To montain the equilibraicm the load acting in 'p' on the lines of action of the axial load. At the based on principle of reperposition.



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Let un divide the nection in to three points then load acting en each post in 'p' only as shown in try

HOM

Here De, , De, 2 Des eye the elongation in small members.

Total Elongation (AL): Al + AL + AL

problem !-

The bar as shown in tig is nebjected to a load of 40 km. Then

- (a) Find the extension of E= 210×103 Hlmn
- (b) Find the young'n moderless value it total elongation in 0.325 mm.

0100

giran data F = 40 KM = 40 × 1000M & \$ \$ \$ \$ \$ \$ \$ \$ \$ 1 160mm x 240mm x 160mm (a) young's modules (E)

= 210×103 H/mm H) $\Delta t_1 = \frac{Ft_1}{A_1 E} = \frac{40 \times 10^3 \times 160}{7/4(25)^3 \times 240 \times 10^3} = 0.0062$

 $\Delta l_1 = \frac{Fl_2}{A_2E} = \frac{40 \times 10^5 \times 240}{\frac{7}{4} \times (20)^7 \times 210 \times 10^5} = 0.145$

Ale = 40×10° × 260 = 0.0062

Total Extension (AL) = Ali + Ali + Ali = 0.0062 + 0.145 + 0.0062 = 0.1574 mm

(b) Extension of portion
$$0 = \frac{FLi}{AiE} = \frac{10 \times 10^3 \times 160}{\sqrt{7/4 \times 25^7 \times E}}$$

Extension of pontion
$$\triangle = \frac{r_{12}}{A_2E} = \frac{40 \times 10^3 \times 240}{\sqrt{4} \times 20^3 \times E}$$

Extension of portion
$$= \frac{FL_3}{A_3E} = \frac{40 \times 10^3 \times 160}{\frac{3}{4} \times 25 \times E}$$

Total Externion =
$$\frac{40 \times 10^3}{E} \times \frac{4}{\pi} \left[\frac{160}{25^{\circ}} + \frac{240}{20^{\circ}} + \frac{160}{25^{\circ}} \right]$$

$$0.325 = \frac{40 \times 10^3}{\epsilon} \times \frac{4}{\pi} \times 1.112$$

problem!
A stepped boy as shown in try in made up of two different matter

The matter of has young's modulus + ax 105 N/mm, while that of matter

in 1x105 N/mm. Find the extension of the boy under a pull of 25kN

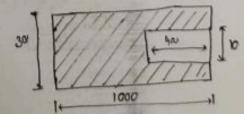
it both the porteons are 20 mm thickness.

Extension in portion o

Extension in pontion (3)

4 boy of length 1000 mm and diameter 30 mm in centrally borred tox 400 mm. The borre dia being 10 mm. under the 1000 25 km, it the extension in 0-185 mm. Final the madellan of elasticity of box.

Length of borred area (L.) . 400mm

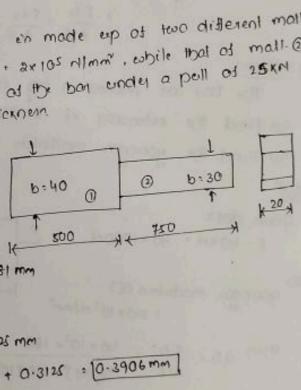


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9999



A1 =
$$\frac{\pi}{4}(30)^2$$
 = $\frac{225\pi}{225\pi}$

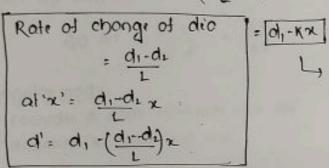
A2 = $\frac{\pi}{4}(30)^2 = \frac{225\pi}{200\pi}$
 $\Delta_1 = \frac{PL_1}{A_1E_1}$
 $\Delta_2 = \frac{PL_2}{A_2E_2}$
 $\Delta = \Delta_1 + \Delta_2 = \left[\frac{PL_1}{A_1E_2} + \frac{PL_2}{A_2E_2}\right]$
 $\frac{P}{E}\left[\frac{L_1}{A_1} + \frac{L_2}{A_2}\right]$
 $\frac{P}{E}\left[\frac{L_1}{A_1} + \frac{L_2}{A_2}\right]$
 $\frac{P}{E}\left[\frac{25\pi}{225\pi} + \frac{400}{200\pi}\right]$

Extension of a topening Rod:

consider a topering bor boring smaller dismeter de bigger dismeter 'd' and length' L' an abown in tig. when the cropp nection varies continiously an elemental length in considered and general expression to elengation of the elemental length derived. Then the general expression is integrated between boundary conditions of length to get total extension.

consider an elemental length dx of the bag at a distance of ix from the larger end.

d = Diameter of the choosen enonnection = d, -(d,-d) x



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crops pectional area (A')= T/4(d') = T/4 (di-Kx)

Shown (e') =
$$\frac{\alpha'}{E} = \frac{4F}{E\pi (d_1-K\pi)}$$

the elemental length dx = e'.dx + strain x length

Total Extension along 5. The first dx =
$$\frac{4F}{FT}$$
 $\left[\frac{1}{d_1 - xx} \cdot \frac{1}{-x}\right]_0^L$

TEX [di-KL di] trom L to/0]

Bet we know that
$$K = \frac{d_1 - d_2}{L}$$

80 Al = $\frac{4F}{\pi \in K} \left[\frac{1}{d_1 - KL} - \frac{1}{d_1} \right] = \frac{4F \times L}{\pi \in (d_1 - d_2)} \left[\frac{1}{d_1 - (d_1 - d_2) \times L} - \frac{1}{d_1} \right]$

= $\frac{4FL}{\pi \in (d_1 - d_2)} \left[\frac{1}{d_1} - \frac{1}{d_1} \right] = \frac{4FL}{\pi \in (d_1 - d_2)} \left[\frac{(d_1 - d_1)}{d_1 d_2} \right]$

AL = $\frac{4FL}{\pi \in (d_1 - d_2)} \left[\frac{d_1 - d_1}{d_1 d_2} \right]$

When the nod in of uniform diameter disdied

&O A 1: 4FL = FL

AE

Rectangular nod:

at a distance x from biol end.

Rate of change of breadth = b1-b2

Area at that enous section (A') = (b,-Kx)+

44

$$= \frac{F}{tex} \left\{ \left[-\log(b_1 - kxL) \right] - \left[-\log(b_1 - kxD) \right] \right\}$$

$$= \frac{F}{tex} \left\{ \left[-\log(b_1 - b_1 t b_2 x L) \right] - \left[-\log(b_1) \right] \right\}$$

$$= \frac{F}{tex} \left[\log(b_1 - \log(b_2) \right] + \frac{FL}{tex} \log(b_1) \right]$$

$$= \frac{F}{tex} \left[\log(b_1) + \frac{FL}{tex} \log(b_1) \right]$$

neoleces from homm A 1.5 m long ofeel bou bamp uniterinitalishiety of homm for a length of 1 m and on next o.5 m its diameter gradually reduces from hom of I'm and the next orson the diameter gradually neolected from hor to so my aboun in tig. Determine the elongation of their bay when nothered to an axial tenals load of 160 KM, given 6: 2009 MIM" pos 1

E= 2009 91m = 2×105 NIMM Total Extension: 100 × 100 × 103 N

Extension on existen partien (DI)

1000

Extension at tapening portion (a)

2 x105x 7x 40x 20 4x 160×103×500 + 4PL Exdide 1 × (40)×2×108 160× 103× 1000 PL AE

0.6366mm 0.6366 mm +

1.2732mm

duper position > painciple of

by each load acting separaof a net of loads and body in the nem of effects counted effect 4 Il Alales that ₹ 8 -tely. Some

Mathematically.

resultant [If R is the P, P&P,] od 'R' = Estect of P, + Estect of 6 P2 + Effect of P3 Feltect

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all theaptive stannes 2 new Hoot 464 stading one linear) materials. ralid painciple in AD in

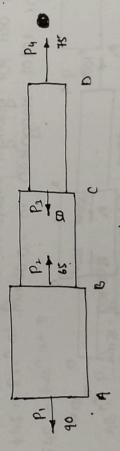
Bain outgreded to varying loads!

section. In new cones load acting in each partition may be tound and the connexponding extensions on each pontion determined. The addition of the bon gires its Boun may be publicated to different loods at different enoun tenal extendion.

·BA The following details netern to a member as shown in problem !-

40 mm x 40 mm, 10c = 30mm x 30 mm, CD = 20mm x 20mm.

pend the total extension. by taxing E = ax105 n1mm 500 mm, BC: 900 mm, CD: 800 mm.

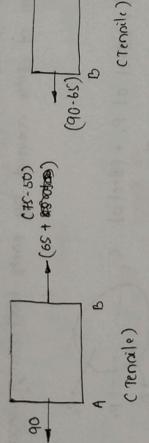


P3 = 50 KM. , Pr. BSKN, 40 KM dince the body in in equilibrium St - = 4d =>90 - 65 + 50 + P4 = 0 => P, + P2+ P3 + P4 = 0

individual pontionn the FIBD of Now drawing

end on fixed V pt. Anouning

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(25-5£)

(90 KM Tenoile) at AB

P

C 25 KM Tennile) 9+ BC

?

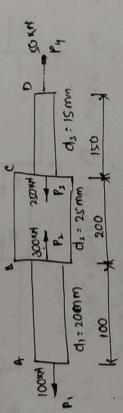
Tunnile) 75 KM At co C:

= 0.14+ 0.125+0.843 Total Extendion: Al, + Ale + Als paroblem !.

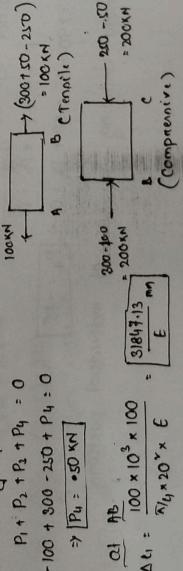
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1.108mm

goengin modelen of the member on whown in teg - 0.04mm. elongation ocal the total when the Frind



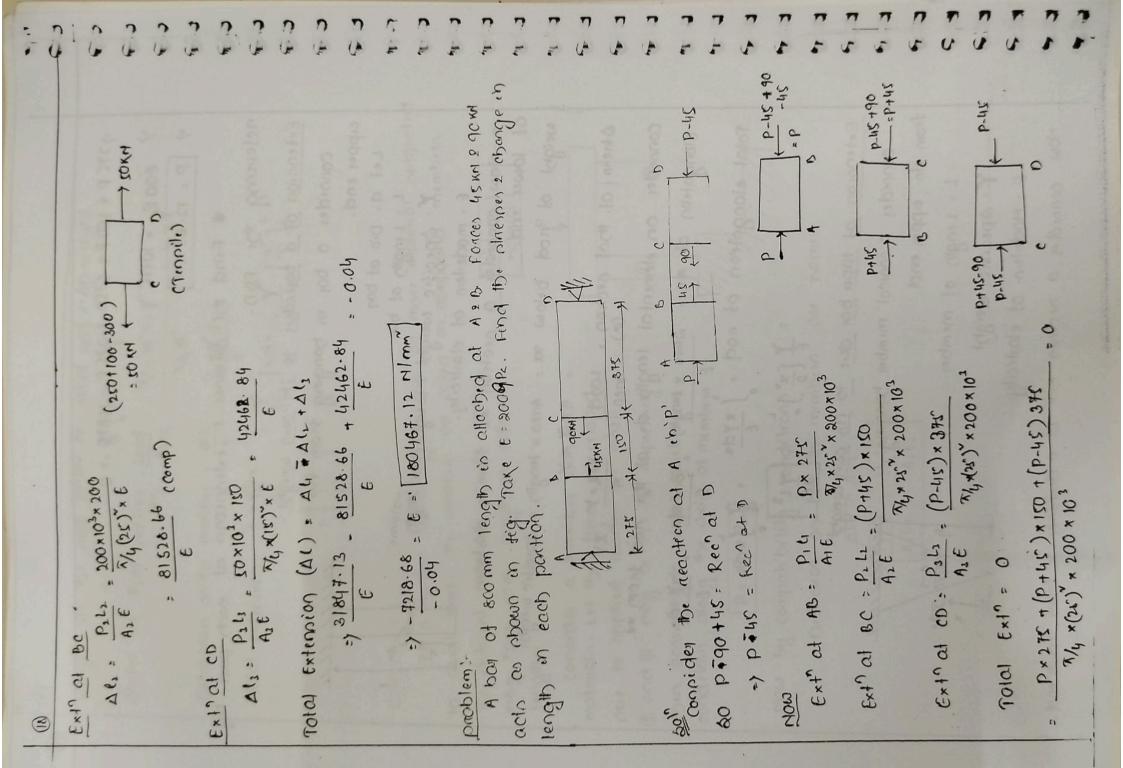
equilibaicm -100 + 300 -250 + P4 = 0 P1+ P2+P4+P4 Conpid ening



Ext

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?



0 " 7275 P + 150 P + 6750 + 375 P - 16875

800 R = 10125 4 P = 12.65 KN

Ra * Find the namenes & extenditions at each post referring the FBD.

boy due to its own weight? Extension of a

7

gram in consider a bay in bonging

cupped end.

r = Length of bon. d: Die of boy

F: Specific weight = weight / until tragity.

Now consider a nection xx from x distance E: moderlen od etooticity.

weight of nod below xx = Aneax length x specific weight = Axxxx

conocides an elemental tength dx at the god trom xx. Stren at that nection: Load Axxxx xxxx xxx xx

7

· Oxex · xp.dx Etongateon at of x = strew x length

4 L2 rotal elongotion of and = Japan

Extension of taper bar due to its own weight

convider a conical member banging snow ith eupper early

lactually of member T: Specitic everybt

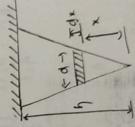
E = Modelen of elasticity

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al a diplence x from lower and. consider o section x-x



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the add below xx: volod add x &p. weight A/12 BUXX 13×Kdx 水水水 *Ox · 13 はdxxxx る。 18 m nection = Load 41 m member = O X YOU'N 36 Total extenoron = Extenperen on the 1001 fo 2 weight Shen

P

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a member consisting of two on mone material perfected one ralled as rempound membern to arial torces. the members Complement Bush

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1-14

4 7

4

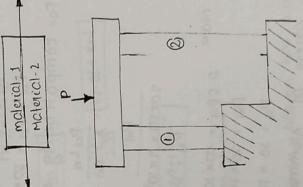
1.

The different materials of the member may have name length of different lengths.

consider a member with two materials. Let the force developed due to applied loads on math.

Band B may be P12 P2 nespectively.

Then according to state equilibrium conditted along the axis of members



p= pi+PL

one name. both the membern conditions NOW by compatibility Deflection on

AL, = AL,

PIL, PIL,

A16, A16,

somm wide x somm thick and a roluip of steel somm wide x 15 mm theax rigidly joined at endo. If the bar in outgrated to a load of soky, Aleminium and the place developed in each material and the extension of the Take elastic modulus of aluminium and pitel as 1×105 Almm A compound boy of length 500 mm consists of a strip of 2x10x MIMMY Respectively. problem :-Porl. ond

L= 50 km = 50 × 10²hl

p= 50 km = 50 × 10²hl

Asl = 15 × 50 = 750 mm

Asl = 15 × 50 = 750 mm

Est = 2 × 10⁵ × 1 mm

Est = 2 × 10⁵ × 1 mm

Est = 2 × 10⁵ × 1 mm

A Load on Alementer (Ps1)

[151 : 151] 750 × 2×105 Pst Lst Ast Est Pst For compatibility Date Ast Pst : 1.5 Pal 201×1×10×0×02 ARI ERI Pal Lay

45.8d

Pair + Pst + 50 x 10 + N

NOW 21.5PAI: 50×10²N

PAI: 20×10²N

PSI: 30×10²N

STRESO OF ALUMINOUM PAREIP:

= 20 NIMM = 20 × 103 1000 A ह

· HONIMA 80×10³ 40 A-g-H Steel Alaip: Shien at

Stacen = (051) = (001) = 30x103 x 500

#50 x 2 x 106
= 0.1 mm

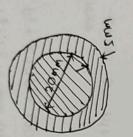
Soke Teach of the sound of the

Paroblem !-

bay conneint of a circular nool of nteel of diamesomm aigidily felled into a copper texts of enternal diometer 20 developed in two material, and threeness smm as shown in Hig. If the bay in oubjected to a load of 100KM. Fend the otherner , Ec = 1.2 × 105 MIMM". ES = BX105 MIMM A compound

AS= 7/4 × 80" = 100 × mm"

Antea of copper teche (Ac) = T × (30"-20") = 1257 mm" External drometer of copper teber 20+2×5 = 30mm for static equilibrium



P= Ps+ Pe from compatibility randition

100 xx 2x105 125 xx1.2x105 Ac Ec Als = Ale Pel As Es => Pst

16

1 Ps = 1.33 Pc 195x 1.2 100x 2

: 42.857 KM => Ps .

2.33 => Pc = 100 NOW, Ps+Pc=100 => 1.33Pc +Pc= 100

Ps = 100-42.857 = 57.143KM

= 181.89NImm 57.143×103 100 A A 12 on pleel (0s) = Sheen

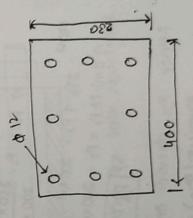
= 109.134 NIME 42.857×103 100 x copper(ac) = Pc Stren on

230mm x 400mm has & ofeel If the column in norbitedial the nationer developed en Es/ Ec = 18.67. A neinsbaced concrete column of pize boun of 12 mm diameter an aboun in try. compression of 600 KM, And modelon natio conorrete. Take to an axial steel and problem !-

8×X × (12)" , [904-779 mm concaete (Ac) = 230×400 - As Anea of wheel (As) = 8x 1/2 x d" Anea of

230×400 - 904.779

91095.221 mm



Pe + Pe We KNOW P =

39 £9.81 x 6 £ £. 406

= 600 KM

5.39 ×93.81 => Pc = 505.88 KM 5.39 Ps = Pc = 8 17 PS = 93.85 KM Ps + 5.39 Ps = 600 KM

= S. 553NImm 103.718 NIMM : 505.88×103 91095.221 93.85 × 103 944.49 2/4 2 con cret. (00) Ac strem on offeel = Streen on Hence

develop Take Ex = 1 x 10 x 11 mm and Es = 2 x 10 5 NImm . what additional poon of and one of steel rupport orcigid Di lloy 1000mm and that of ofteel pilloy in secmm Find the otherness . If onea of each alementem pillons, two of alementical of sooky as obsern in feg in each pillon. Two problem!platform 600 ç

working stresses are esalon

en pteel? toke it

Total tonce .. Pat Pst Pa = 200 KN SOCKN => 2Pe + Ps = 200x 100.d> to Dare to 100/

800x 8×105 Psx 250 2 Pa = 0.78 Ps => Pax 280 ... 200×800×2 250×1000 condition Ps Ls As Es 2 A13 =1 Pe = Ps AaGa Alc Pala Compatibility

Pa= 60.78KM 200 KM 2x0.78Ps + Ps = 200xN => 2.56Ps = Ps = 70.04×4 2P2 + Ps = 200 KM MON

= 60.18 H Imm" 60.78×103 1000 2 Alemium (Pa) = the otherner are 1-tence

W: 200KM ied 1 JOGWH

94.55 Almi 78.04×103 000 Ps/As Stel (as) =

DAXA = 65x 1000 = 65000 N BS NImm Aleminiem (OA) = Aleminem (Pr) = Additional load 'p' > 100 000 T othern at

* 83,333.33 N. 6x000 0.48 0.48 0 Load on rateel (Ps) =

65000 copocity, apa + Ps 2× 83333.33 + Buyanios boot lator

= 231666 N = [231.66KN

Additional load (P) , 231.66 - 200 = 131.66KM

Alemenium(Pe) = 0.78 Ps = 0.78x 1,20,000 = 93,600 M. on pleel (Ps) = 05x As = 150x 800 = 1,20,000 A Afeel (05) = 150 Almm sheen at Load on Locd

3×93,600 + 1,20,000 eapacity = 3Pr + Ps Burging . Total load

** 3,04,200 " BOOTENER (304.2KM)

307.2- 200 = (107.2 KM) Additional load (P) =

problemi

Riguesono 30 mm and external diameter 30 mm. The length Take Es = 200 GPE, centrally through a copper oppositioner of the after tight filting of the oped the 2mm. diameter pannen pitch of quarter of in sto mm. tube, ed Ra A roteel bolt of 16mm diameter whole annembly bolt and 1.2 × 105 01 mm. tabe of enternal cy ned induced 0f the £ 0 3 ₹

Ps= Force acting on order (Tenoile)
po = Force acting on copper compression)

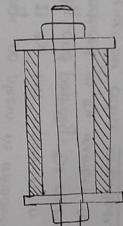
Ps+ Port 0 => Ps=-Pe

Let the foace acting in 'p'.
Deflection At = 1/4 pitch = 1/4 x 2 = 0.5mm

thy tebe aboutened. over Highteners 2 dere An the bold extended

net deflection

Alet Als: Al = 0.5 mm.



392-699× 1-2×10×) = 0.5 AcEc 3 2 0.5 = 392.699 mm 201.662 × 2×105 + 7/4 x16" = 201, 062 mm * 107-91441 mm => p = 31697 .331A Anec of copper (Ac)= 7/4 (30"-20") 005 x d 6 AL: ALS + ALe : 0.5 81694.33 201.062 Anes of seel (As): PL

contracto when ebonge en length en dinectly proportional to arines every material expands and also tempreture change (41) length of member and tempreture tallo. The when tempreture Tempreture Strennes!

55.252 NIMM

21697-33

392.699

90 : A

AL & LAF

P

97

0

7

2

9

material due to change an enit tempreture where & = co-efficient of thermal expension it in detribution an change in anit length

If the changer due to tempnetate are permitted freely no chresnes develope enthe member due to encueare in tempnetare the born will extend by att. due to this ethonge no chresn in chroduced.

If the face expansion is prevented fully and pertially, the chresnes are introduced in the member and these chrosnes chances are called tempnetare chresnes.

0

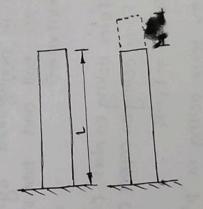
0

0

?

consider a bar as shown in try. If the bear is there to extend puppent torce p en have Duevented completely to forces develope at supports. The effect of when tempreture in increased by it a been att. But if the extension in

a tendency to compress by oft.



(3) Kothy 00 portially Here of in the tempreture when and it is compressive in nature. prevented ey PlA = ONE At => Out out att-8 as oboun in Fig-6 then member in A: 0411-= ANDAF A: WILAT PL 13 P PE PE Hence

some plandarid values.

Expannion, of Menmal 19×10-61.0 17.5× 10-4/01 18×10-6/06 23 × 10 -6 10c 12×10-6/0c coefficient BROMP, BRONZE Stainlen oteel Aluminium Material COPPU Steel

of 200°C. A niteel nail of 15 mm long and in laid at a tempretent tempretene expected in 10°c The maximem

gap between two noils to be lest no temporetene stresses do not develop. minimum € → Entimate

nails et C+ 42 calculate the thermal otheropes developed

as no expansion joint to provided.

7 Is the slaes developed in asmilim". what in the gap less bet the exponotion. gap in provided son If a 2mm \$

20/9-01 x SI = 2.1 × 105 MNIM" and a 4

nails?

= 15×10-6× (40-20) × 15× 1000 -> The dree expandion of the nails = at L = 4.5 mm

+ E: SSILLEHAM + B.IXIOSANIM" - B.IXIOS NIMM"

P

1

12

1

lay 19 no expansion joint in provided, since expansion restricted in 45mg

6.e AL = 4.5 mm

(b) If 2 mm gap is provided (8=2mm)

0

10

7

= as n1 mm" and 8 in the gap places developed in 25 milmi \$ 1 F

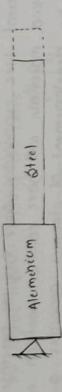
boy in nigically titled at the nupporth A & 13 as aboun at the nephondo when tempreteur naines and , Es + alsgallm", da + 12×10-6/0c As: 300mm Speel 4 Aa = 600 mm the neactions by stee. Take Ga : 75 GNIMY Aleminium A componite en Jeg. netermine 043 + 15×10-6/0C. paroblem?

53

n n n n n n n n n n n n n n n n



C



The state expansion would have been

= 12×10-6 x 24 x 1000 + 15 x 10-6 x 21 x 1000 = Ora Alla Tos Alle

0.324 + 0.81

Since this is premoted 11: 1:134mm It p in nupport nearlian the AL: = 1.134 mm

E. = 75GAIM PLa + PLS AREc ASES 1.134 = P[1000

- Es = 215 × 102 M/mm ~ #5x 103 MIMM ~ # 103 MM 1m

1000 600x 75x 102 + 2000 800 x 200 x 103

1:134 = P x 5.55 × 10-5

P = 20412N

between two ungielding support at a orm tempareteure, what in the movimen ntreso indicced in the ben, if tempretere rather by 30°C of take Es-2-1x10x A steel boy unithamly resigning in diameter as shown in styl held Mlon", OS = 15 × 10-6/00 Example!-

d, : Gomm how in STE OF THE STE => 15x10-6x30 x400 = [0.18mm Face expandion of the bon = AL: ON WALL

7×30×60× 21×105 = 0.18 p in the tonce developed in nestricting the expansion 1 4× P× 400 AL: 4PL

=> P= 0.18xxx30x60x2.1x105 1 × 400

P= 130506.724 1

U

U

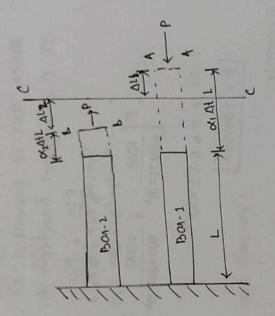
U

Pount Y in compound Temparetone Stresses

mestice int developement of otheron. consider a compound a compound bay neparating, the two materials will have common position which is one prevented from bon of length 1. The aire en temprietuse in Al. a, 20, one the elastic modeles. two malerials of different tree expanacions conce, by 0) Demal expansion and ELL Es are De when temporeture aises the Ra Rivo experience Donorble

Let a, Ya,

Free expansion of bone 1 = 0, 111 expannion of bon 2 = 0, 111 develope in bon-1 while tennile 0,011 + DL, + 0,011 - DL, Now a compression rotano will As a, ya, no a, all ya, all of pon-2 Pi= Pi= P souce will develope For equilibrium From the Higher



DL, + ALI : 0141 L - 0,011

+ PL. : (01 -01) A1L AIEI

ALG. + ALG. | = (01 -01) AFL AI EI AZEL 10

A) EI Az EL (d1 - 02) A11 x

(d1-02) At (AIEI + ALEL) (A) E) + A1EL) 1 7 D: (MANAGE)

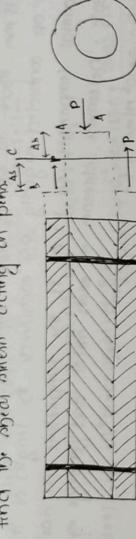
(Tennile) (dwos) (AIEI + ALEL) (COI - OL) At (A161+A262)(Q1-02) A1 ALGIEL staenou in boy 1 (a1) = PA1 bon 2 (on) = Plan દ Shen

problem!-

steel tebe of tomm diametal (external) and 30 mm internal diametal. The base and the tube both eneticily 1.5 m long and are aignily toolened ofaction in bay of botons 30 mm dicemeter in enclosed in a Fend the dicemeter pehro. 20 mm both endn by

10xe Es: 200 KNIMM, Eb: 100 KNIMM, OLS: 11.6 × 106/°c, 06: 187 × 106/°c ton molerials cohen temprietene native from 25°c to 45°c

object when octing on pina. Also And Me



NOW, L + 15M = 1500 mm

At = 75° - 25° = 50°c

46= 7/4 x (30)" = 106.5 mm"

As= 7/4 x (60"-30") = 2119.5 mm"

Es: 200 × 102 4 1 mm 100×102 NI m~ [P :

CABAIL - ALB : OGAIL + ALS

DLb + ALS: 000 AIL - 05 AIL = AIL (06-05)

DIX (9-11-1-81) x 0051 x 05 = 10 As Es Ab Eb

\$ 0.5325 2119.5×100×103 PL Teb.5 x 200 x 103

3285.0 : 7 px1500 [4.07 x 10.9 + 4.71 x 10.9] 2 Pb = Ps = 30135 - 82 H 1500 × 11.78×10-7

= 42.65 NIM" Athero in Dacon (02) = Pb : 30135.82 200.0

2 14.21 NJmm 30135.81 2119.5 States in steel (05): Ps

Since when the pin will obsen it will obsen at two double open. nections no it in the case of

2 0 00 0 C 1:3 0 (8)

G

U

14 OCABLY H OCATY

, Es= 2× 105 NIMM", Ec= 1× 105 NIMM", , L = 1.2m = 1200 mm given date,

1

10

1

0

045= 12× 10+10c , 04c= 17×10-610c

position tenoile touce will act on steel and An ar yas so ALE Y ALS But plates one nigically fastened. = 360mm As: 70x15 : 1050 mm", Ac: 45x8 baing them to tenal

Again Ps = 2Pe [An two copper plates and thouse] compressive torre will act on cappen.

OCALL - ALC = OSALL+ ALS

=> ALe + ALs = OCAIL - OSAIL # (ac - as) At1

ASES Peto + Pst Ac Gc

7

17

1

[An Ps = 2Pe = (ac-as) At L Pet + 2Pet

) = (ac-as) At AsEs + 2Pc Pe

(17-12)×10-6 x 80 61 1050x 2 x 105 7 1 360×1×105

?

17

2

9

5 × 10 6 × 80 9.52×10-1] => Pc [2.77×10" +

21493.82 H Pc = 10746.94

21493.81×1500 1050x 2x105 = 12×10 ×80×1560 + = 20.47 NIm~ 29.85 NIMMY change in length of compound bay : asall + As = 1.595 mm 10 746.9 21493.82 1050 360 ALES = 05A11 + PsA = 1.94 + 0.155 Pe , 2 × Aluen en coppet nod (on) . Sheen en pleel nod (0s) = 0

A boarsonld aligid boy weighing HOKN in bung by threevertical as objects on mods each of orgin length and usomm' enons section Pacblem!-

The central rod in mode of wheel and the outer radio are copper. If the temprietere nine in soic estimate tond will descend the load commied by each ned and how much the

J. / 501 x8 1 = 2x Ec = 100 GAI m 06/ 201x5-1 = 2x Es: 20094/m" Toke

reise if the entire load 170x1 is

be the tempretente pleel alone? 200 what smould to be convied Spirin dato

= 2×105 NIMM Es: 200 GNIN" = 200 × 109 NIM"

: 1×105NIMM Ec: 1009 MIM : 100 x 109 MIM

(e) when only 170km 100d will act! 1:0.9m. = 900mm

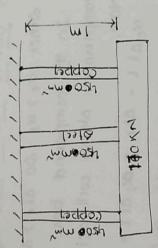
punoduos o vo The enitial ebonge en longth in The repley behaves weight How. 4 · loog

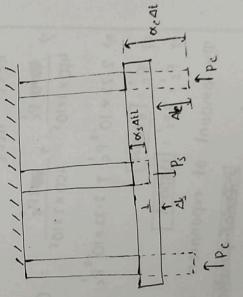
Extendion in oleel Extenden in copper : Ps + 2Pc = 170KM

300

3

ALS





NO0

2Pc+Ps = HOOKEN 17844

=1 2Pc+ 2Pc = 100mm 170 mm

=> Dc = 42.5 KM

=> Ps: 2Pe = 85KN

= 0.85 mm 85 × 900 × 1000 450x 2x 105 AsEs Pst Extension due to loading =

50°C of Due to aire in temp by 50 Ale > Als منادد طد ٢ طع

and act on noteel In the compound boy tenoile atteno will

compressive stars will act in copper.

OCALL - ALe : OCALL + ALS

copper dux to temp.

Pc = Black On

Note:

Ps'= Shen on

ofeel dece to temp.

DLe + DLs = OREATH - OREATH

1

= (ac-as) At L + Ps.L. AcEc Pcl

= (ac - as) At ASES Pr + Pc

05 x 201x (2.1-8.1) 61 450 x 2 x 105 h 450x 1x10st 1

12

17

12

R

7

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= 0.6 × 10°5 × 50 2.22 × 10 8 Pc + 2.22 × 10 8 Pc

=1 Pc = [6750N

Ps = 2Pc = [13500M

= OcAll + ALe of expansion olve to tempreture mine 0,411+01.5 X SON A PORTINGO The amount

= 0.6615mm 0.54 +0.1215 41 500 x 7 x 005 006 x 00561 + 006 x 05 x 5.01 x 2.1 = 05.01.1+ P3.L

+ Ext dec to temp reine rotal length by which the bay will descend: Extr der to load

0.6615 1.5115 mm 0.85 +

17

Load connied by wheel bon = Ps+ Ps' = 85000 + 13500 = [98,500 M

Load countied by each copper ad = Pc-Pc' = 42500 - 6750 = 35,300 M

50

113

110

13

(m) Rine in tempreture is entine 170 km load in to be condied dus

Extension due to load 170KM , Exta due to temp reine. => Ps" = 170KN = 170×103 N by okel ned

2 4. FS1 = = 1.2×10"5 × 1 450×2×105 ×1.2×10-5 = 01 × 01 => 130 × 103 = 450 × 2× 105 170×103 = 05 A1 L = 1 At = . As x Es Ps" x L

Exercine problemos

Shear! Simple

A moderial in noid to be in a plate of primple pheap if it is subjected to only obtaining othern. Objecting force takes to object

of the enone occition of body. peut obtain as oboun in trig. Consider a ball subjected to

consider a small enonnection of that element.

Let the enternity of obear when be it is consider the equilibration be gab and thickness of element of element

(Element under Strail) 9 9 vertical force on cD: ged x cDx1 vertical tonce on 48 = 9x ABxt

Pad

now ton balaneing

6 = geb x CDxt => gab = grd gab x Arb xt

also parallel to each o'Der no tot form one couple along moment Now gab & god one equal en magnètude and opposite in direction

1.e = gob x ABx 1 x AD -0

will generate ite for baloneing thin couple another one rouple of the tig the tig the tight. another one muble

9 Mx ADX 1x AB = 9 x ADX 1x AB so couple tormed by these torces in Let 960 = 900 = 91 - 13

81 10 Pes 9:91

1.1. The element offers a risear of intensity of amon the ABCD. Lel Br Mconnen connider a plane 186 at an angle 18 with the face 18c. Now ना क्रांत मुख्य प्राची oblique pection when element connider on elemental nectangular block faces AB & CD and the faces AD & BC. Stremes in

the Jonces acting at the wedge nection 18EE ctg-d)

7

(i) Force goodlang be J

Force gx Ec along ce ->

(cir)

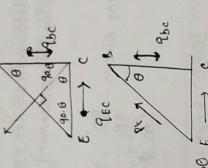
Force Py normal to plane BE

Resolving the forces normal to plane BE to plane be (e) Force Pt tangent

gxBcx ding + gx Ecx long -- 6

Resolving the torce, along the plane BE **(1)** gxbcx cong - gx Ecxome -

on: Py : 9x Béaing qx Et cong Normal phress acting on plant BE



9x cono. Sino + 9x sino. coo 6

000

= 29 AMO. CCOB = 900 MAD = 18

व काग र छ rangential

of que same 9.BC. CCOB BE at: Pt " BE

: 9. cono. cono - 9 amo. amo = 9 (con o - amo)

U

6 = 9 con 20 -

on 9 : 9 sm28

Hence Mo normal and tangential stresnes at plane 186

9 00029 5+5

Stn 10 - Hence to plane conaging maximum normal stren to þ ment value Noter

7 Am 20 = +1 => 20= +90° => 0= +45°

(+ for tenoile 2 - for compressive)

Thence the plane extere my normal othern in maximum when when ρğ meint

For maximem rater of object others the conso values mentbe zeno.

U

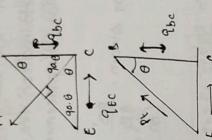
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5

=> CONZO = 11 => 20 = 0001 180°

=> 0: 0. 04 do.

6 C 9

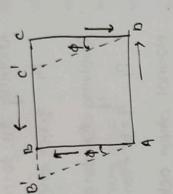


aimple obean tennile whiers of name magnifiede developes at 45° to obseauting plane? टका व्य sheen משלש " BUNGONIA

b = . Shxcusb = Orus b = 40

Straing strain!

Steering stress bas a tendency consider an elemental enous section Aber distant the body to a parition Add D. This deformation in expressoral interms angular diaplacement and called as shown in Hig.



Observations BB: 1000 + 0

(As \$10 very omall)

poranion'n Ratio:

force the length of boy increases connespondingly alno changes. For example Is due to tenale a material undergoes change en one dimenpión connesponding other dimenpion iln enonmection decreases.

The natio of change in length to original

It in found that with in elastic limit there in a constent matio of change in enonnection to omiginal enomnection in latural name. between lateral strain to linear strain length in linear stading. Bimilary the natio

on poinnion'n natio. 31 in denoted by 1/v on 12. For most metaln its lies Deteusen 0.25 to 0.33. Linea strain

anignal volume in colled as volumetric a member in nubriched to tonce it endergoes change bionce the volume of member changes. The natio Volumetaic Strain: dimen sionn when

change in voleme to strain.

volemetric strain (ev) = change in voleme

Strain of a Rectongular part volemetac

0

5

Let a rectangator bar bareng length: 1, enderge Dieadly: 6 & Mickney + + Mag At romall obange of At, Ab 2

Original voleme: 1xbx1

Fenal voleme . (1+a1) x (b+ab) x (1+a1)

()

. 3

0,

113

+ 41×45×41 + 1x bx at + bx at x at + 1 x abx at = (xbx++ Alxbx++ 1x+xdb+ Alxabx+

Trencelled on [lowo Binx

= 16+ + bxtxAt + 1x1xAb + 16xAt

bxixAlt lxlxAbt 1xbxAl chonge in volume

113

volemetaic strain = bxt x At + txt x Ab + lx b x At

= | EL + Eb + EL = EV 1 + 4b + 4t

volumetric Strain : strain in length + Strain in breadth + & train in thick-

Volemetric Shain of Centulay bon?

connider a borr of length it and diameter Ad one obsorge on length and diometer. id and Al and

Original volume = 7/4 d" L

8/4 [dx+ Adx+ 201 Ad] [1+ Al] Final volume: I cd+ Ad) C(+At)

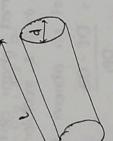
74, [drt 2.0. Ad. 1 + dra 1 + 20, 20 de]

change en roleme = The [dil+2.d. 1. Ad + dial] - Fhy oi'l

= Ny [2.0.1.20 + dral] 7/4 [2-d.1. ad + arat]

volumetric strain =

7/4 01 DE 417 2. 40 + volumetric strain = abounge in length + 2x strain in dicmeter.



constants Elastic Elastic

and book modulen and Modellen of elasticity, modellen of rigidity

Horee elootic conplantin.

elasticity: It in the natio between unear nines to + Moderlen of

E= 0/6 linear statein.

It is the noted between obey others to shear rigidity! 04:5 + Modelen of stacen.

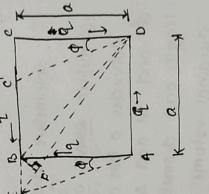
booky neubjected to identical ninezoes (0) olineation the books employed obange So Buk modulus in the natio between identical In dencetion to volemetraic strawn. -> Bely modelessi- when a all mederal perpendirector metually states in three roleme.

modelen of elasticity & modelen of regidity. Deteneed Relationopip

"×

convider a nguare element ABED of nider deformed phape due to pheory, Let the obten ص robeal of intensity Due to application of load AEC'D in phoen in a 2 modulum of aigidity q. to point nubjected

Let an observe the strain along the diagonal [Drop a 1a BF on ED no that BD = FD 00 PB DE - OB =



[AD DB = ABJE] ABAE. can be anounted 00 18ED .. Angle of detormation of in very small on 45° . So lott = 45° Hence EF = DE Con45°

BE CODAS. Q. 12.12 a-tang. 1 ABVE ABVE EF a tang con45° Atrain in diagonal BD = A5 52

= a tand => BE = AB tand BE tand = DABE

[An \$ +0, tang · 12 4 77. 1/2 tand

tenoili oladen en dereloped en diagonal Bb in developed in AC. Let the tendile when के ए वि poods other Dec to compressive along the length 300 and

77

17

210 中十十年 Tennile alawn along 180 :

(741)

(1+1) es, 0 c0 2 × 4 Equation

consider a cobic element rectified to niners a in Mare markeally Reightonopip between modellen of elasticity and Beik modellen:

perpendicular direction x, y, x, as aboun.

phen on in a direction eacher tennile P in x-dire-- etécn estile Now the

की कीमतरा हा य- diaection

y Or 5

> (WZ-1) 62: F (1-24) gimilany

volemetaic state

3(1-241) 30 (1-174) E=3K(1-24) Bulk modulun(K) = 0

6 = 29 (1+4), 6 = 3x (1-24) NOW

= 3x [1-2(Eq -1)] = 3x [1-2E +2 NOW, E : 3K (1-24)

98

F1 3

6

Ox = On = 02

-

· E(9+3X) 9 +3K 9x - 3x6 0/5 , E greg 9+3K E: 3K [3-E] E + 3KE · 日 ·

20 mm diameter in tested in tenxion. It in observed that of 37.7 KM in applied, the extension measured over a of 200 mm in 0.12 mm and contraction in diameter in 0.0036 mm, Pend pornoion'n matric and elastic constantin مارم م الموط o bod b Problem ?-

7/1×(20)" = 100 x mm" d = 20 mm => A= Thy d" = P = 37.7 KM = 37700 M

gauge length(e): 200 mm

At: 0.12mmm At: 0.0036mm

Ad = 0.0036 mmLine col | color | AL | color | color

0.0006 0.00018 0.0036 20 Loteral strains Ad :

0.00018 Lateral strain Linear sharm poinnion'n natio (ש):

200004. 71 Mlmm 0.12× 1007 37 700× 200 PL " ey E = 引出 We KNOW,

= 76924.89 NIMM 200004.71 2(1+0.3) 29 (1+4) => 9 = E " E Mon

176924.89 MIM 200004.11 we get G: E

= 1166670.59 NIMM 3 (1-2×0.3) 20000 4· #1 6:3K C1-24) 41 K = E 3(1-24) From the relation

7

14 14 1,i en serbj aigidity, bolk modelles and chonge in volume is poincions -ected to a tennile fonce of 1000xM. Determine modellen of Prx V = 25.4648×10°5 × 7 × 0× 1. gno1 mm 002 = 1.667 × 105 11mm = 0.7692× 105 Mmm = 127.324 NIMM = 63.662 × 10-5 2×105 MIMMY. 1000 mm2 C1-2×0·3) puo , 62 = - M. C. 3×(1-2×0.3) ×1/4×100 5.01x8494.52 diameter 1000 × 103 127.324 nated = 0.3 and ejoung's modelers E 2×105 2 (1+0.3) volumetaic standing (ev) = ent eytez 2×10 ×5 2×105 5.01 × (99.69 = = ex (1-24) Original volume change in voleme : change in valence Lateral Stawn (eg): - Liex A centerior nod of 100 mm Linear Aran (e.) = Stren Longitudinal stron: P/A 3(1-24) E= 29(1+4) => 9 = E E= 3K(1-14) 3K = E 64: Pachlen!

1,4

13

14

15

14

1

-

bey of each necked 20mm x 40mm. the change in volume if E= 2×105 MInm" and e1003 peompareneire there on homm x coomm fores. tennelle torce on 40mm x 500 mm faces. Tennelle toace on 20mm x 40mm forces. A 500 mm 100g acciengular thin boy in newspected to Find 40 KM 200KN 300 KM paoblem! 一

*

4 "

All the tonces in member one meterally = 50 MIMM " 15 M) mm 20 MI mm 300×10° 40×500 200× 103 40× 103 20 4 500 20 × 40 perpendicular 2 An 四型 P2 .. *6 1 76

.

P

1.

$$e_{3} = \frac{e_{3}}{E} = \frac{e_{3}}{E} + \frac{\mu^{2}}{E} - \frac{\mu^{2}}{E}$$

$$= \frac{1}{E} \left[50 + 0.3 \times 20 - 0.3 \times 15 \right] = \frac{51.5}{E}$$

$$e_{3} = \frac{e_{3}}{E} = \frac{e_{3}}{E} - \frac{e_{3}}{E} - \frac{\mu^{2}}{E} - \frac{\mu^{2}}{E} - \frac{e_{3}}{E}$$

$$= \frac{1}{E} \left[20 - \mu \times 50 - 0.3 \times 15 \right] = \frac{39.5}{E}$$

$$e_{2} = \frac{e_{2}}{E} = \frac{e_{2}}{E} = \frac{\mu^{2}}{E} + \frac{\mu^{2}}{E} + \frac{e_{3}}{E}$$

$$= \frac{1}{E} \left[15 = \mu \times 50 + 0.3 \times 20 \right] = \frac{e_{2}}{E}$$

$$= \frac{1}{E} \left[15 = \mu \times 50 + 0.3 \times 20 \right] = \frac{e_{2}}{E}$$

problem :-

A boy of rectangular rection shown in try in nubjected to streme Px, Py and Pz in x, y and z directions respectively. Show that if the norm of these stresses in zero, there in no change in volume in the bon.

All the tonces are acting mutually perpendicular to each other.

$$e_{Y}$$
: $e_{X} + e_{Y} + e_{Z}$

$$= \frac{P_{X}}{E} (1-2\mu) + \frac{P_{Y}}{E} (1-2\mu) + \frac{P_{Z}}{E} (1-2\mu)$$

$$\frac{\Delta^{V}}{V} \cdot (1-2\mu) - \frac{P_{X} + P_{Y} + P_{Z}}{E}$$

$$= \frac{\Delta^{V}}{V} \cdot (1-2\mu) + \frac{P_{X} + P_{Y} + P_{Z}}{E} = 0$$

$$= \frac{11}{V} \cdot \frac{P_{X} + P_{Y} + P_{Z}}{V} + \frac{P_{Z}}{E} = 0$$

0 = V 1 /=

i.e. Myere to no volumetric change if Px 1 Py 1 Pz = 0

pachlem:-

and modelles of aigidity in tound to be 0.78 x 105 MIMM. Deleymine poincing to be 2.1×105 In a tennile test young's modules of moll is tound

E = 2.1x105 NIMM, G = 0.48×105 NIMM

=> 2.1×105 = 2× 0.78×105 (1+ A) 1000, E = 29 (1+ 11)

=> (1+1x) = 1.346 => (x = 0.346

3x 0.308 = => [K = 2.2 HSx 105 MIMM" 6= 3x (1-24) => 2,1x105 = 3x (1-2x0,346) Again

A material has modules as aigidity equal to 0.4 x 105 mm and bulk modules to 0.75 x 105 mm . Find its youngs modules and poinnion's notion

3x0.75x105 + 0.4x105 9×0.45 × 105 × 0.4 × 105 , K = 0.75 × 105 ~ 10mm voing the nelation 9 = 0.4×10 × NIMM 9x46 . .

- 1.01 × 105 Ham

2.7×1010 2.65×105

> => 1.01×105 = 2×0.4×105 (1+41) E = 29 (1+4) Agom,

(1+24) = 1.26

when the external force is applied on a body 110c body offers nevertanden the external force is applied on a body 110c body offers nevertanded it developes felly about about deformation in the work is Maxm sheen + yield when glood a gd panolic and non change by a body consider a member of length is and enon protional areo in in publiched to a fonce ip: Let the resintance at any mament to (60) P+O x el : 1/2 pel shaffet Pago . 12 ner = 1/2 x stren x strain x volume shan energy per enit volome in called Revilience = KOAEL = Koex permanent deformation in called work done by newhoting tonce = Arg. newhance x De shain energy in the body = w. o by resinting tonce Defrancter ance and it developes telly when deformation 10.02 × = 12.02 Revilience : 8E deformation in At = el, R:P 2 9 , S when determation in zero, R:0. nestinance tonce in dreams body deming whosining in called the tonce. This tonce arranged in the body interm \$0 the energy referred in the Strain Energy? Rexilience thin energy bungs words when the loadin 9·6 without endergoing coonc The maximem Enong Rextience? body back. 7.66621. Paxilience? Rexilience. Kemoria when

the colloy the tead traveln a diplonee Al. stron enorgy othered : 4 th wany done by load = with All = w[b+ez] . w[b+@] W [5+ 9 1] = 12 9 AL Chod Buttonies

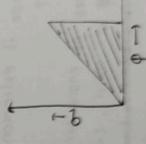
SKWOK ARK

ALAL

o" = SEW [h+#1] .

1xdx Gerraert) 13 x 9xBCxIx ABX & Bx NEZ P

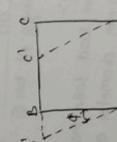
15



Tee'r Ae Icno OT G X ABX \$ G = dx Bc xt

workdone by the force = garg x DB

straing force a acting on face be. 4 chin 9:9.



throxnen't'in nabytelted to alreaning developed in zero when 9=0 and in othern 'g'. The enternal olasin

connider on element Abon of

about load in measured intering of energy. So about lead applied in a member let be u unit. The plans packered in the bar

Key Shory loads-

Ribinos of Glim Bridge Conta

can be obtained by equaling to

A SEU

20 41 = U = 7

produced by shoek load.

(Sincer) energy dere to obear others!

-b1 v br- 420 ded with the equation in the form of ax't bxtc = 0 riegethy solution in not considered on we +1(21) +4 SEWH 0 = 1 80 - 1 (A)" + 4 REWIN SEWN . O places volue O. 1 - (-30) P. 1 88. 9 Equating ששששששש

(1)

2

1+4 36 M

1 4 AM + AM

3 x 3 1 [11 11+ 3649

4 [14/17 SENA

30 mm

20mm

30 mm

300mm

boun of nome material as aboun Maximen places produced rame (b) 1000 applied load in compose the strong enough of for 60 gradually problemi-

[2x(47.77) x x x (20) x 200 + (191.06) + = x (10) x 500] A0 01: 93 + (OL) VL + (O3) V3 4299.23 N-MM 1 [2x0, v, + 0, v, (O) V, 2×2×105

shown energy stoned in the member: Energy at 10 + Energy at 10 + Energy at 10

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, 191.08 NIMM Stann in eachern (2003: P/Az = 15×1000

hyth wimm x4 x(20)~ 15×1000 caons section O = on= PA ج Staesn

NISKN \$ 20° 1 \$10 @ rocmm ф 30 LOCKIM 0

with eincentar anonneation in new Jeated to a load of 15km the chain energy stored in it take E: 8×10 + 11mm \$ Determine problem !-

= 1/9×0×1 = 1/9×0×1 = 1/9×0 = 1/9×0

Alach energy aboved: workdone by internal othernes 12 x abrear others x abreal phrain x volume. work done =

bon of 30 mm dicompeter and 400 mm long. Find the contantenteuro when and 4 100M 10ad Jalla from a beight of 60mm on a collar attached to a of enten if extendion of the bon in neglicited in tenal wonk done by extension produced on the bon: Take E = 2x 105 MIMM. what in the paoblemi 1000l

5

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21666.67 . [3.11] @ wa to BBHO3 O was to BBIADS

shain energy at bon @ = oi"vi + oi"vi = (4/9 0) × # x(30) × 300 +

Stann at dia 30 mm; 040: 0×42 , 0×74,×(20)"

Now, stacen energy at bor 0 : or x x x (80)"x 600 = 645000 x 1 4 ph " Box Maximum staten is at diameter 20mm 1: e: 0,20

Let maximum othern is a, do maximum othern at bon 0 = a when maximum when produced in name:

= 0.615 0.6897 × P/E 0.4244 x P/E 4 Doy (1) Energy. of bon @ Energy at

Pr [0.2122 + 0.4775] = 0.6897 Pr

3 1 1 2 1 1 2 1 1 2 1 1 2 1 1 2 20) × 4 60) × 300 1 (1 2 20) × 200) × 200] Stanin energy started in ton 0 = Energy at 0 + Energy al 0

strain energy atored in bon (= 1 × vol = 1 / 1/30) × 1/4 × (30) × 600 = px x 0.4244 (e) when applied load in name 180

6

$$\frac{\sigma^{\nu}}{\partial E} AL = w \times h = y \quad \sigma : \int \frac{w \times h \times 2 \times E}{4 \times L}$$

$$= \sqrt{\frac{100 \times 60 \times 2 \times 2 \times 10^{5}}{225 \times 4 \times 100}} = \sqrt{\frac{92 \cdot 132 \times 10^{5}}{100}}$$

-1 rage ethan in approximating

$$= \frac{92.273 - 92.132}{92.273} \times 100 = 0.1537$$

- Instantaneous extension produced $= \frac{0 \times L}{E} = \frac{92.132 \times 400}{2 \times 10^5} = \frac{0.1842 \text{mm}}{10.1842 \text{mm}}$

P8 . 25

4

...

Inhoduction:

eglanders and opheres are commonly used as components of machinaries and chemical plants and encoting they are subjected to internal and external presneves. Cylindern can be classified in to two cologonies

-> Then eylinders on aphenical abell: - when the thickness in less than Vioth to Visto of its radion on 1/20m of diameter then it in called then eylinder. Here addial stress in small so neglected.

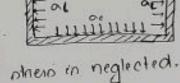
+ thick extended and appealed abell: when the thickness in more than Noth of modition on 150th of diameter then it in collect thick cylinder. Radial states in taken in to consideration,

otheres in then eglindrical obellat

A thin eylindrical obell in oubjected to tollowing otherner.

(+) ciaccimpencial olaers on book others

in Longitudinal othern (au)



An the thickness is very small no nodial shess in neglected.

this constitutional phoens.

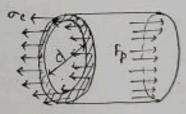
Force acting on the easts of the eglander Fp . Pox My d' = pax Anea

Resinting torce at the cylinder wall FR= Maxt x ac -0

For equilibrium

PX To X +x Ox +x OL

The starm which in acting along the length of the explinates in called longitudenal nteen.



P. Januar pressure of their d. Dia of rylinder. t = threanen at eglinder on L= Storen at annexemble from

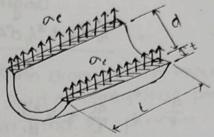
it) Concernderencial when coo!

The stress outsich in acting along the circumserence in called circum--defencial othern

Florid tonce acking due to priesnere:

Resisting touce acting on cylinder walls:

For equilibrium, Fp: Fa



P. Pa of flourd t = thickness 1 : Length of cylinder

Hote! while designing the cylindrical shell circumstencial places in considered because its value is more than longitudinal stress.

Change en dimension of cylindrical obell:

Now, ciacamterencial strain (ec): oc_ 1000

$$=\frac{1}{E}\left[\frac{3d}{2t}-\mu\frac{Pd}{4t}\right]=\frac{Pd}{4t}\left[2-\mu\right]$$
be the change on dimension

Let '8d' be the change en dimension

Equating 1 2 8

Let 'De be the change in length

change in volume : Final volume - Original volume

-

-

-

```
- change in volume (AV) = exx V = 7-497 x 10 9x xxdx L
                 . 7.497×10 9× Tx (1000)× 2300
                        = 1177704.54 mm3
Ducplew :-
      A thin cylinderical abell, 2m long her 200mm diameter and incorner
et metal 10mm. It in titled completely with a tland at almospheric pressure
It on additional arose mm3 though in pemped in , tend the premiere
developed and boop & longitudinal ninein developed. Find also change
en diameter and length. Taxe E= 2x105 n/mm, L1 = 0.3
  L-2m = 2000mm, d= 200 mm, t= 10 mm, AV = 25000 mm3, E= 2 x 105 n1 mm2,
 60 \text{ or} = \frac{Pd}{21} = \frac{P \times 200}{2 \times 10} = 10P
      O_{L} = \frac{Pd}{4t} = \frac{P \times 200}{4 \times 10} = SP
 Concumplemental Main (ec) = pd (2-24) = px 200 (2-0-3) = 4.25 x105 P
 Longitudinal strain (ei) = Pd (1-24) = px200 (1-2x0-3) = 1x10-5 p
```

volumetaic stacin (ev) = Av , 2ectel = 2x4,25x10 p + 1x10 p = 9.5 × 10 P

$$P = \frac{48 \times 10^{-5}}{10^{-5}} \times \frac{10^{-5}}{10^{-5}} = \frac{10^{-5}}{10^{-5}} \times \frac{10^{-5}}{10^{-5}} = \frac{10^{-5}}{$$

change in diameter (Ad) = ex d - 4.25 x 10 5 x px d = 4.25 x 16 5 x 4.18 x 200 - 0.035 mm

change in length (AL) = eLXL = 1×10-5 × PXL = 1×10-5 × 4.18 × 2000 : 0.084 mm

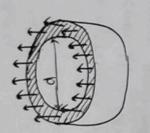
Then opherical abell?

Foace exerted by enternal Horid of the 3 Junction (Fp) = Ty, d'xp

Residence tonce exerted by the obell

For equilibrium es" (1) = es" (5) (FA): Axdxt x Ox

(2) Axdxtxo1 = AxdxP P0 # 3



(1-1) 101 - 21 Ot - Ot (1-41) = Pd cincompenencial phrotin (e.) = Ad Shawn! -

volemetric olacin (ev): Av : Final voleme - Oaigenal voleme original voleme

43+3: 4 (20) +30" Ad + Ad -= 3 ec 340 30,40 93 7 d3 \$ x(00+00)2 7 d3

(1-17) 3Pd 4te RVI

and change in diameter and ASSMIMM, ASK I IMM, Take E= 2x105MIMM, egaphenical obell has diameter tromm volerme edyen flexist presoner in morreoned to enderced and thickness 10mm. Find the othern At atmoopheric presoure, a thin problem?

D= 750 mm, t= 10 mm, p= 2:5 NI mm, E= 2 × 10 5 NI mm, L = 0.35 46.875 MIMM - Hoop when (O4): PD : HON BASE 580 : m

Pod (1-12) rencomperencial phoeninger): 200 = 1

change in Diameter => Ad = pd/ (1-4) = 2.5x(450) (1-0.35)

+ volumetare phaariles). Av : 3Pd (1-41)

100955. 11 mm2 change in volume (DV): 3Pd (1-4) x & d2 (1-0.35) × 1/2 × (750) 3x 2.5x 750 4x 10x 2x10s

were accorded of their cateday. cylinders are strengthened by clonely winding wines under terrior. when the cylinder in acibiected to internal their presners then the walls of the cylinder are subjected to tennile load. It the cylinder in enitially loaded by winding the wines by compressive load then due to tirul the tennile load developed compensate the the admit of their compressive load then atten compensation tennile load developes. Hence of eglindrical walls increases. This techcapacity of eglandern in encially adopted for those -niger of placengibening materials which are not very strong in tension (cost Iron) and in neigh cone steel evines one eined.

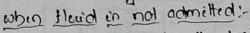
Let d' = Diameter of steel ovine. Francoccepange

Diameter of cylinder Thickness of cylinder

Length of cylinder

aw: Initial tennile street on

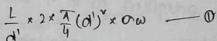
or: Initial compreniere places on cylinder.



Let un connider the half of cylinder. Fonce exented by one tenn of cylinder =

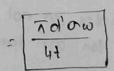
2× 1 x(d) x 0w No. of turns of wines at allength L= 1/9'

Total fonce exerted by the wine wounding :



Resinting tonce on the cylinder = 2x1x1x0c

ton equilibraicm eg 10 = eg 10



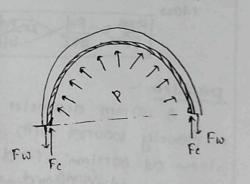
when fluid in admitted!

Let the pressure developed due to theird pressure only

Owa = In wine

oca : In cylinder

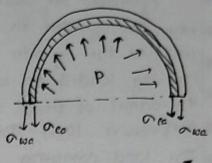
considering the torce acting at half portion of cylinder

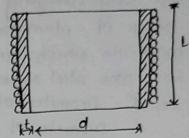


Fonce acting on wine 2 cylinder

Fonce due to water prespure

For equilibraion 3 = 4

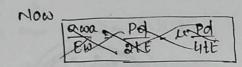


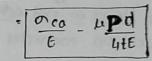


Strain:

An wine and cylinder both one rigidly fixed no ntrach in both cylinder and wire are nome.

shown in wine (ew): ow [Ew: young's modelus of wine]





paoblem :-

A 250 mm diameter et pipe has metal thickness of 10 mm. It in clonely wound with 6 mm diameter steel wine with an initial Atresa of 80 Mlmm. Find the timal atresaes developed in cylinder and wine when flowed in admitted in to it with a presnure of

Take Ec = 100 KN/mm , L = 0.3 and Es= 200 KN/mm

d= 250 mm, t= 10mm, d'= 6 mm, ow = 80~11mm Given data

Length of cylinder in not mentioned no Let un connider ton a length of 6mm for one tean of wine.

Fonce exerted by the entropy wire at diameter of cylinder.

(5)

tuited alarm on eylander.

Atten the fluid admitted:

now drain equation

$$\Rightarrow \frac{\sigma w^{2}}{2} = \sigma c_{0} + 5.625$$
 $\Rightarrow \sigma w^{2} = 2\sigma c_{0} + 11.25$

By polving two equations

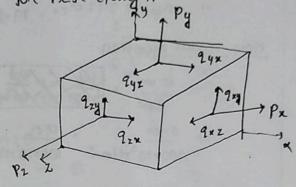
final Strenes:

Introduction:

A structural member may subjected to different types of stresses (normal 2 obearing) otherner nimultaneounly. It in therefore necessary to tend the region cobere the effect of these intremes will be critical from the design point of riew. When nuch othernes act at a point in a stresped material, there always exist three arthogonal planes where exists entirely normal stress cwith no shear stress). Such planes are called principal planes and nuch ntresses are called principal stresses. One of these phincipal stresses here greatest value called maximum principal othern and one in baring lowest value. The maximum principal should not exceed the permissible value for note design.

Streenes on an Inclined plane!

To tend the stresses acting at an inclined plane we consider à general plane at an inclined angle e to the known plane. In that plane we use to tend out normal and tangential components.



The tollowing three types of stressed condition in an inclined plane in considered.

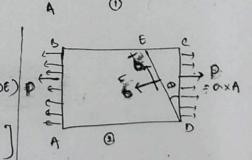
- tor uniquial direct stress
- (b) Bianial direct street
- ser general two dimensional stress system.

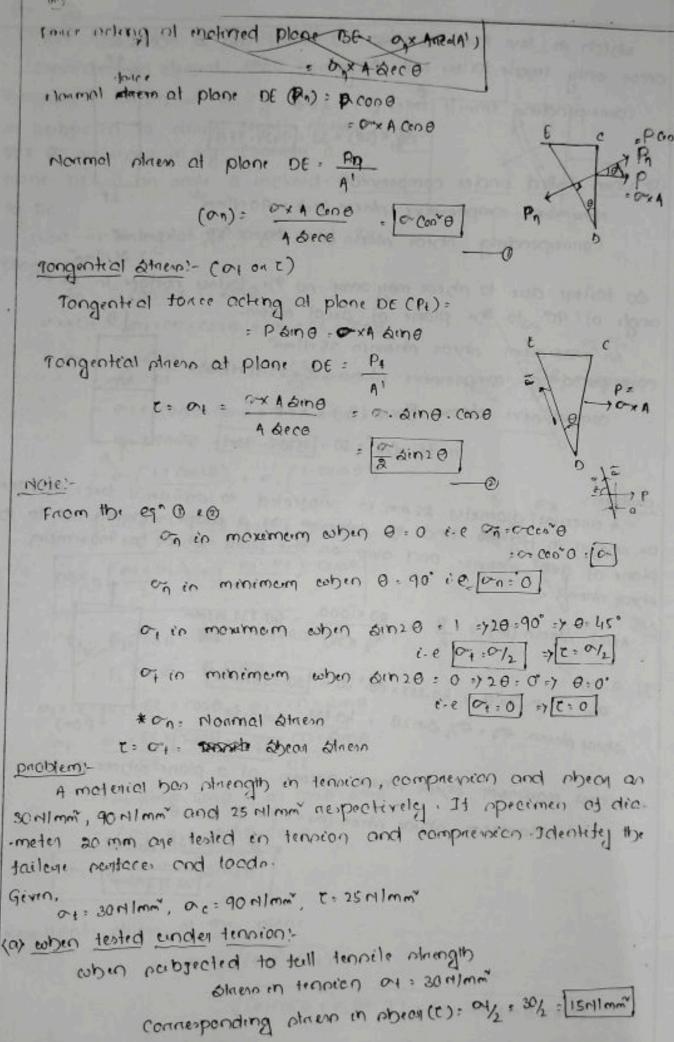
Elementa publicated to unioxial direct stress!

connider an element subjected to diaect unioxial strem. Let un consider a plane at an angle 8 to the plane CDIH i.e DEFI

Let un analyse at 20 nystem en tigle) Let the load acting on plane cons = P

Anea of plane = A Stress on plane (a) = P/A enon nectional area of inclined plane (DE) pt A1 = A sec 0 Front DE





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100

LP

450

which in len than 25 Hlmm no tailers due to obear will not occur only tennile tailers will occur. corresponding tennile tonce (P) = Ax a

= 7/2 × (20) × 30 = 9424 - 77 H

(b) when tested under compression:

Maximum compressive placer (ac) = 90 Hlmm

Connesponding obean othern (t): 0%: 90%: 45 mlmm > 25 Mmm

so tailour due to obean may occur no the tailour neutore in all an angle of 45° to the plane of axial states. 1 Pc

An maximum obean othernin 25 Hlmm connexponding compressive others 25 x 2 : sorthand comprenere places Ponce (Fe) : Axoc

17/4 x(20) x 50 . 15+07 . 93H

A cincertag diameter as mm in publicated to an oxial torce of 20KN problem : as abown in tig . Find the placemen on a plane making 30° to the plane of axial atresnes and also on the plane which has maximum obean other - -

Axial Atresa (a) = $\frac{p}{A} = \frac{20 \times 1000}{7/6 \times (25)^{\circ}} = 40.737 \text{ H/mm}^{\circ}$

ση: σ coo θ = 40.737 x coo 30 = 30.558 NIMA Jf 0: 30' shed when of = 01/2 sin 28 = 40.737 x sin 2.30 = 17.643 Mlmm

we know maximum obean othern occure at a plane where 8:450 Manumum about atten (at-t) = a bin28

Elementa publicated to Bioxial Direct alread-

connider on element Abob baring theorems 't' an abown in tig. It in acubjected to direct tennile alamous 12 12 as abown in tig. Consider a plane DE at an angle 8 inclined to DC.

Now resolving all to torres w.n.1 the

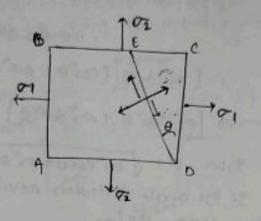
$$= \frac{\sigma_1}{2} + \frac{\sigma_1}{2} + \frac{\sigma_1}{2} \cos 2\theta + \frac{\sigma_2}{2} \cos 2\theta$$

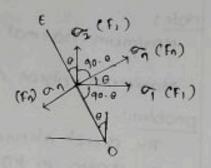
$$\left[\sigma_{n}: \left(\frac{\sigma_{1}+\sigma_{1}}{2}\right) + \left(\frac{\sigma_{1}-\sigma_{1}}{2}\right) \cos \theta\right]$$

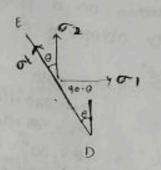
:- az ame. cone + ai cone. ame

$$\sigma_{+} = \left(\frac{\sigma_{1} - \sigma_{1}}{2}\right) \sin 2\theta$$

Resultant stress at the plane







= [0, (00, 0 + 0, 6, 10 + 20, 0, 6, 10 6, 00, 0 + 0, 6, 10 6, 00, 0 + 0, 6, 10 6, 0, 0 6 6 6 7 0, 6, 10 6, 1 - 20102 xin 0. con 0) 2

=: [01, could (could + 810,0) + 01, 810,0 (810,0 + could + could)]

· [() () () + 0 ; 2 () 2

then as Voicoret or sing

If the angle between nesultant others 'a' and given plane in o then tong : an los

Maximum normal shess (00) mex ((01+02) + (01-01) [8.0] riote :

Moximum about atheracon mix: this . 1/2 (01-02) [8-45]

problem !-

The direct strenger acting at a point in a strained material are as shown in try. Find the normal, tangential and the resultant phresses on a plane 30° to the plane of major principal others. Find the obliquity of the resultant ameso also. 1 portium

given data 01 : 180 H1mm

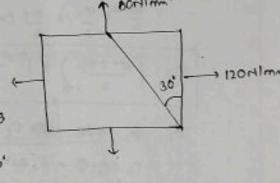
01 = 80 N/mm

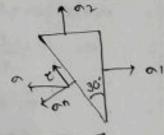
Normal othern (on): 01+02 + 01-02 con20

rongential on object othern (ort)(1) =

Resultant ation (a) + V(an)"+(r)" + V(110)"+ (17.32)" = [11.36 N1mm"

Angle to malined plane \$ = tan" (on) = tan" (ho) = tan" (ho) = 81.05





problem :-

The direct others at a point in a strained material are looking. compressive and souliment tennile as shown in tig. Find the sheeper on the

plone Ac.

given date

P1 = 60 Mmn

P2 = - 100 Mm (comprensive)

$$\frac{60 - 100}{2} + \frac{60 - (100)}{2} = \frac{60 - 50^{\circ}}{2}$$

= 31.423 Mlmm

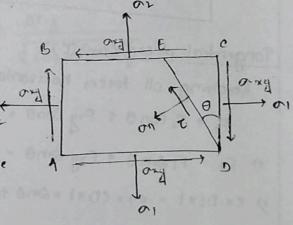
$$\sigma_1 = \frac{\sigma_1 - \sigma_2}{2} \sin 2\theta$$

Elemento oubjected to general two dimensional which ogsten abicxis! Maein combined with obed othernil-

Connider an element Abon subjected to on 2 or nearmal phrenes and try, obean street as about in tig. Connicles a plane at an angle 8.

Let on : Normal strens on inclined plane

t: obear othern on inclined plane.



F. .

Note:

Here the assumed directions for on a, on 2 tay one taken as the direction changes the stresses here to one med ponitive. It as negetire.

Monmal when (an)

Let the thickness be 't'.

Bringing all the torces to the plane DE

4 Godina 100 MJ mm J 60Hlmm

$$= \left(\frac{\sigma_{1} + \sigma_{2}}{2}\right) - \frac{(\sigma_{1} - \sigma_{2})^{2}}{2\sqrt{(\sigma_{1} - \sigma_{2})^{2}}} + \frac{2\pi i}{\sqrt{(\sigma_{1} - \sigma_{2})^{2$$

Maximum obeca other in delived in the page : (70)

60 Hlmm

60 Mlmm

Horlman

180 N/mm

problem !-

The state of stress at a point in a strained material in as about in tig. Determine

ce > The direction of the principal planes.

cay the magnitude of principal stresses

cer the magnitude of the maximum shows stress and its direction, indicate

all the above planes by aketch.

given data,

+19

3

o1 = 100 Hlmm, o2 = 60 Hlmm,

Ezy: 40 Hlmm

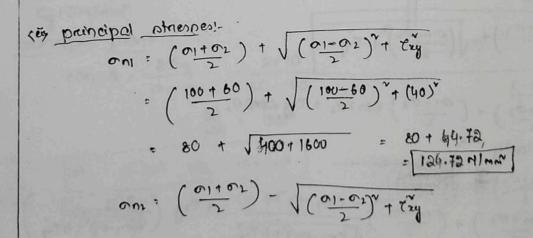
(i) The direction of the principal planes; 100+1mm

$$tan 2\theta = \frac{2try}{a_1 - a_2} = \frac{3x40}{100 - 60} = \frac{80}{40} = 2$$

20 = tan-1(2) = 63.43

0: 31.71

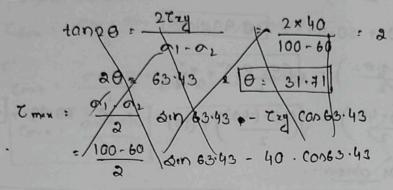
81:31.71, 8, 01+90:121.41

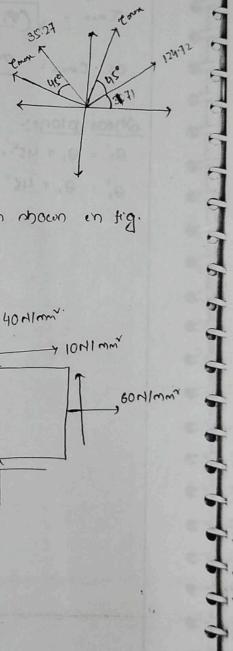


$$= \left(\frac{100+60}{2}\right) - \sqrt{\left(\frac{100-60}{2}\right)^{4}+(40)^{4}}$$

$$= 80 - 44.72 = 35.27 \text{ H/mm}$$

(Maximum about atacon!





problem:

In a strained material the torces acting are an aboun in tig.

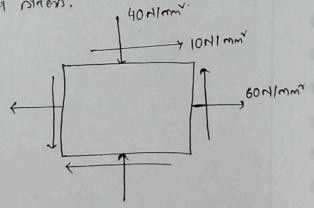
- Determine -> principal planes 2 principal atresnes
 - Maximum obeal otherner and planer
 - Resultant almennes on maximum shear almens.

girin data 01: 60 HIMM", 04 = -40 HIMM" Cig 10 NImm

principal plane:

$$ton 2\theta = \frac{2c_{ny}}{o_{1} - o_{2}} = \frac{3 \times 10}{60 - 40}$$

$$= \frac{30}{100} = 1131^{\circ}$$



(comp)

$$\begin{array}{lll}
& \circ n_1 = \left(\frac{\alpha_1 + \alpha_2}{2}\right) + \sqrt{\left(\frac{\alpha_1 + \alpha_2}{2}\right)^2 + \frac{\alpha_1}{2}} \\
& = \left(\frac{60 - 40}{2}\right) + \sqrt{\left(\frac{60 - 40}{2}\right)^2 + \left(\frac{60}{2}\right)^2 + \left(\frac{\alpha_1}{2}\right)^2} \\
& = 10 + 50.99 = \frac{60.99 \text{ All mm}^2}{2} \\
& = \left(\frac{60 - 40}{2}\right) - \sqrt{\left(\frac{\alpha_1 - \alpha_2}{2}\right)^2 + \frac{\alpha_1}{2}} \\
& = \left(\frac{60 - 40}{2}\right) - \sqrt{\left(\frac{60 - (40)}{2}\right)^2 + \left(\frac{10}{2}\right)^2} = 10 - 50.99 = \frac{-40.99 \text{ All mm}^2}{2} \\
& = \left(\frac{60 - 40}{2}\right) - \sqrt{\left(\frac{60 - (40)}{2}\right)^2 + \left(\frac{10}{2}\right)^2} = 10 - \frac{10.99 \text{ All mm}^2}{2} \\
& = \left(\frac{60 - 40}{2}\right) - \sqrt{\left(\frac{60 - (40)}{2}\right)^2 + \left(\frac{10}{2}\right)^2} = \frac{10 - 50.99}{2} = \frac{-40.99 \text{ All mm}^2}{2} \\
& = \left(\frac{60 - 40}{2}\right) - \sqrt{\left(\frac{60 - (40)}{2}\right)^2 + \left(\frac{10}{2}\right)^2} = \frac{10 - \frac{10.99 \text{ All mm}^2}{2} = \frac{10 - \frac{10.99 \text{ All mm}^2}{2}}{2} \\
& = \frac{10 + \frac{10.99 \text{ All mm}^2}{2} = \frac{10 - \frac{10.99 \text{ All mm}^2}{2} = \frac{10.99 \text{ All mm}^2}{2} =$$

Maximum about others;

Thex =
$$\sqrt{\frac{(60-40)^{2}+(0)^{2}}{2}}$$
 = $\sqrt{\frac{(60-40)^{2}+(10)^{2}}{2}}$ = $\sqrt{\frac{50-99}{100}}$ = $\sqrt{\frac{50-99}{1000}}$ = $\sqrt{\frac{50-99}{1000}}$

Manner phear phreat

no two preincipal streemer are an ears then the plane of mar obean will always lie 0,+45° x 0,+45° (0,+135°) with the redesence plane

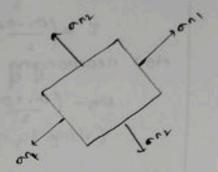
THE WHATH OR BERTS OF HEALTH

Hoxemom phear stress

$$\frac{T_{max} = \frac{\sigma_{n1} - \sigma_{n2}}{2} \delta_{in20} - t con20}{t_{max} = \frac{\sigma_{n1} - \sigma_{n2}}{2} \delta_{in90} - t \times con90}$$

$$\frac{t_{max} = \frac{\sigma_{n1} - \sigma_{n2}}{2} \delta_{in90} - t \times con90}{t_{max} = \frac{\sigma_{n1} - \sigma_{n2}}{2}$$

A SUCCE PROOF SOIL SPANE SAID



Mobin cencle in the graphical representation of stress system. It was proposed by german Civil engineer of Mohn in a developed technique

we know that,

$$\sigma_n = \frac{\sigma_1 + \sigma_2}{2} + \frac{\sigma_1 - \sigma_2}{2} \operatorname{con}_2\theta + \operatorname{try}_3\theta \operatorname{in}_2\theta$$

$$t = \left(\frac{\sigma_1 - \sigma_2}{2}\right) \sin_2\theta - \operatorname{try}_3 \operatorname{con}_2\theta$$

Now rearranging the equ

$$\sigma_{n} - \left(\frac{\sigma_{1} + \sigma_{1}}{2}\right) = \left(\frac{\sigma_{1} - \sigma_{1}}{2}\right) \cos 2\theta + \cos 2\theta$$

$$\tau = \left(\frac{\sigma_{1} - \sigma_{2}}{2}\right) \sin 2\theta - \cos 2\theta$$

equating and adding both equations

Thin in equivalant to the equation of circle (x-h)"+(y-K)" = R"

so thin nystem can be represented by a circle.

procedure ton drawing Mobils circles

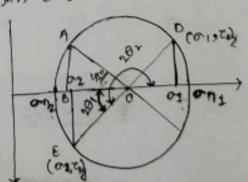
-) consider a co-ordinate nystem by considering normal when in x-axin (tre right nide) and obear othern in y-axin (tre-towards down nide.).

- Find the pointh ocar, ty and Ecaz, etg on the co-ordinate nystem.

- your the identified points and locate the point where it in meeting with x-onin.

- By considering on as nadion draw a circle.

- The cincle in called as Mobile cincle



3

Observations

 $\alpha_{11} = \text{Radium of cencle } \left(\frac{\alpha_{1} + \alpha_{2}}{2}\right)$

on: $\left(\frac{\sigma_{1}+\sigma_{2}}{2}\right)$ - Radico of cincle

A opai , op : Radium of circle

201: Angle of on, 201: Angle of on,

20,+90°: Angle of maximum about attens 1 20,+90:=20,+180°: Angle of maximum about attens 2.

AB: Maximum obeg others (It is nadius of circle)

Note:

- Consider a proper scale (eg 1041mm = 1 cm) to draw the circle.

+ For them them (by downworld direction in considered as -ve. because angle 20 in considered as +ve when counterclockwise.

othernes at any plane at any angle can be tound and tog drawing

a line at an angle want the line DG

of the connesponding x-anin value will give the normal stress and the y-anin value will give obear others.

problem:

By considering the datas of the problems noticed for analytical

approach solve tox metan circle.
(2) Given data on: 100 Hlmm, on: 60 Hlmm, Exy: 40 Hlmm

0(01,27)

72

The late

0

oni

10

(02, Em)

From the tig.

on: 126 4/m2

ans = 35 M/mm

201: 63°

20, : 243

Tour : 45 Hlmn

From Analytical,

on1 = 124.72 Nlma

ans = 35.27 Alma

28, : 63.43

281: 248:43

Cmex = 44.725 H)mm

problem - 2

girm date,

01 = 60 mlmm, 02 = -40 mlmm, 2xy = 10 mlmm

(0,,tm)
(0,,tm)

from the tig

on = - 41 Alma

012 = 61 M mm

281: 11°

202 1910

Chex = 51 NI mm

From Molytical

On : - 40.99 HIMM

om: 60.99 Hlmn

201: 11-31*

282 191.31"

Cmax: 50.99 Hlmm

The plane on which shearing attain in zero in called preincipal plane. Similarly to tending principal almentes, we can tend principal attains in attained material, it we know direct attains and obtaining attains on a plane that makes an angle w.a.t contessed direction and of years of the plane that the plane of an attains on a plane that makes angle is a set the plane of an attains.

- : Shearforce and Bending Moment Diagram:

Introduction:

+ statically determinate beam:- A beam in naid to be statically determinate its reaction components can be determined by using equations of platic equilibrium only.

ΣF = 0 , ΣM = 0 , ΣW.D = 0

7 Types of beams!

THE PERSON AND THE PE

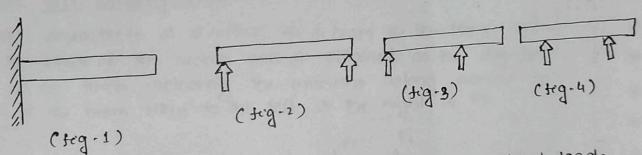
(a) <u>Contilered Beam:</u> Then type of beam in tixed at one end and three at the other end. (trg-1)

(b) simply supported Beam! when the ends of the beams are made to treely nest an repports in called simply repported beam. (tig-2)

(c) Overhanging Beam: The beam which in having tree ends atter the neupport in called overhonging beam

-> single reide overbang (tig-3)

+ Double ride overhang. (tig-4)



Beam: Beamn are the horizontal members that support vertical loods (tennon, compression) on, moments and bending.

<u>Calumns</u>: Columns on the restrical members that support axial and lateral loads (compression) 2 moments

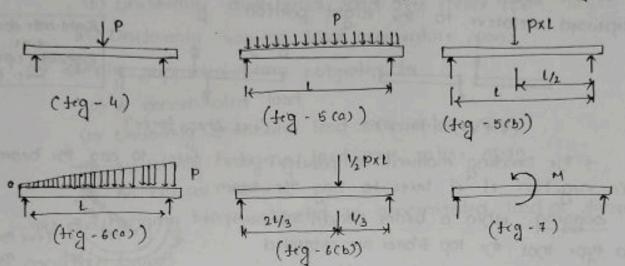
- Types of loads usually beams one subjected in transverse direction! (e) concentrated tood: It the load in acting at a point. It is

also called as point load. (fig-4)

(b) unidonnly distributed load: It the load value is some throughout the beam called UDL. Its value is detended as load acting per unit length x length of the beam. It is supposed to act at the centre of the loaded pencen. (fig-500),500)

(c) uniformly ronging load: If the load value varies uniformly through a length in called UV.L. It is value in numerically equal to the area under the load and it is nepponed to act at the geometric centre of the area. (trg-600),600)

(d) Externally applied moment: It any moment in acting at any point in the beam directly it in collect externally applied moment (trg.7)

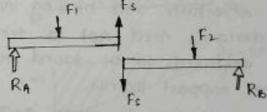


try 606): convention of UVL in to point local.

Sheartonce and Bending Moment:

sheartonce! - objection or a nection in a hearn in the tonce that in adapting to object of the nection and in obtained as the algebraic norm of all the tonces including the neactions acking normal to the axis of the beam either to the left on the right of the nection.

shear tonce (Fs) = Rq - F1 = Rm - F2

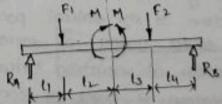


.

Bending moment: Bending moment at a nection in a beam in the moment that in triging to bend it and in obtained as the algebraic num of the moments about the nection of all the forces cincluding the reaction acting on the beam either to the left on to the of the nection)

Bending moment (M) .

RA(11+12) + F1 x 12 = RB(13+14) + F213



3

3

dign convention:

the obeau torce and bending moments are the vector quantities and the tollowing night conventions are generally used.

-) The obeau torce in ponitive if it tends to move left particon Right nide downward

appealed relative to the right partion.

(+ve shear torce) (-ve shear torce)

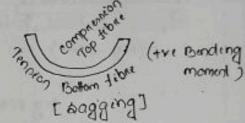


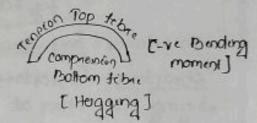
Rightide operad

-> The bendeing moment in positive it it tries to mag the beam and in negetive it it tries to Hog the beam.

sagging: when a beam bendo in such a type that the top tibres are nubjected to compression and bottom tibres are publicated to tennion.

Hogging: when a beam bends in such a way that the bottom tebres are subjected to compression and top tibres are publiched to tennion.





sheartonce & Bending Moment Diagrama !

objectionce and bending moment values vary from section to section. A designer need not to trind out of Rom at all the points ball it in required to be tound out at rollient points i.e. at all load and aupport points.

A diagram in which x-axis represents about torce and 4-axis represents about torce in called about torce Diagram (SFD) and x-axis represents load and 4-axis represents bending moment in called bending moment diagram (BMD).

From any OFD & BMD tollowing things can be tound.

- rates at the datient points, i.e. maximum, minimum and the paints where nature of variation changes.

- Notege of variation between national points

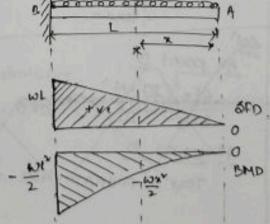
+ Location of point of contradlexcure i.e. the point where binding moment changes it righ obviously value of BM: 0.

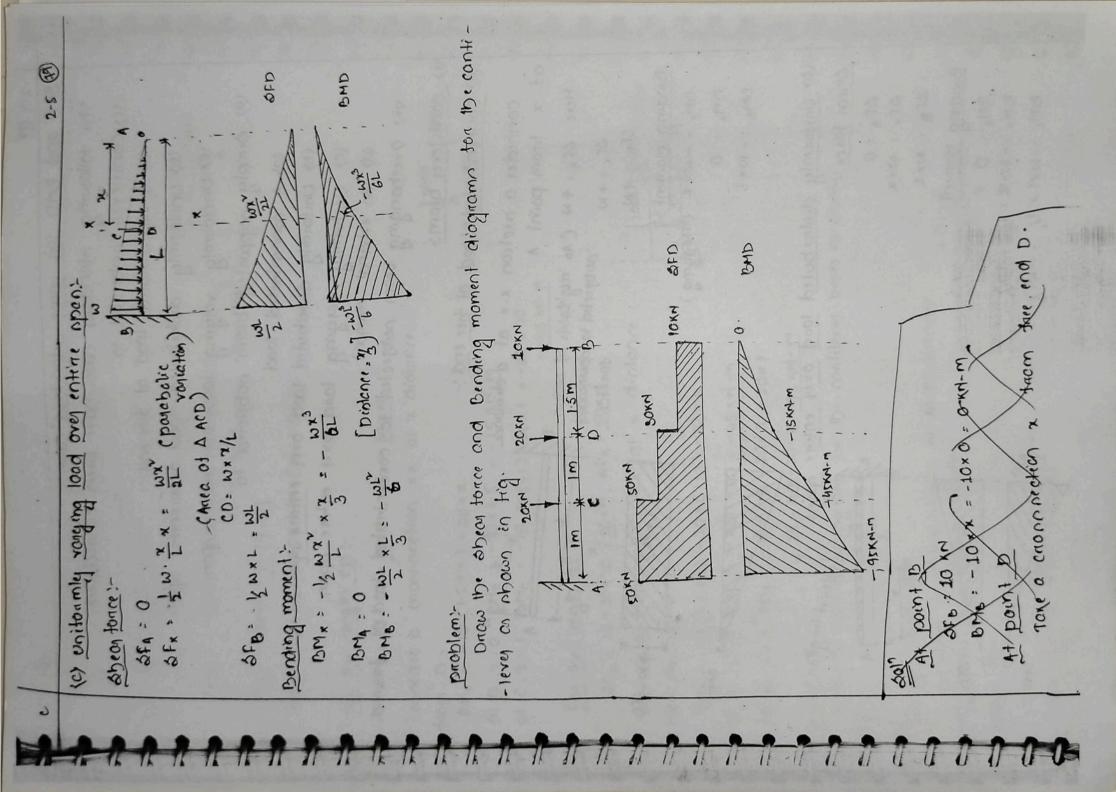
Bonding Moment:

BMA = 0

BMX = - WXX x 7/2 = -WX/2

BML = - WXI x 1/1 = - WIX

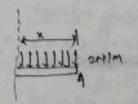


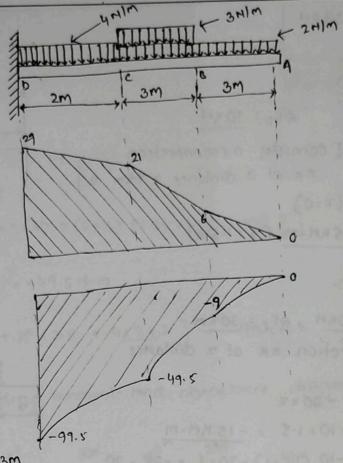


sig.

For the length AB connicted a enough pection xx at a diplance a from the tree end. shear torre

SFx: 2xx N SF4 : 2×0 = ON [x :0]





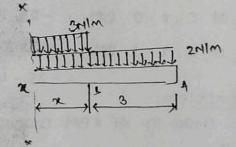
Beiding moment

$$BM_{\star} : 2 \times \times \times \frac{x}{2} = \frac{2x^{\star}}{2} \quad (Hogging)$$

For the length BC

shear tonce

Bending moment



- [10x3+(20x4)+(2x4x412)]=|-166N-M : -30 KI-M -[10x3 + (20x0) + (2x0)] SFc = 10+20+C2x0) = 30 RM 10+ 20+ (2x4) = 38 M BMB. 5Mc

- [10x9+20x6+2x4x2+2)+30x1 = -30 2 N-M 10x (#+x) + 20(4+x) + 2x4x (42+x) + 30xx] at A, x = 2m 2FA = 68M 10+ 20+ 2x4 + 30 KM BM9: BHE= 1- 166N-M x = 0 35x = BMx : \$ 13p ल के

104

Simply Supported Beam?

Ra + Re = W
Taxing moment about A
Rex (= wxa =) Re = wxa

 $R_{B} \times l = \omega \times \alpha \implies R_{B} = \frac{\omega \times \alpha}{l}$ $R_{A} = \frac{\omega b}{l}$

a pechion xx in between Be BMe = Wa x b = Wab N.mm BMB: WG x0: 0N-mm considering nection xx between A BMx : REXX E SFx =- Rx = - Wa SFC : - WA N ~ MO ~ Considering aff. क म्छ S T S

SFx: Rg: WB BMz: Rgxx: WB x

at A, x = 0

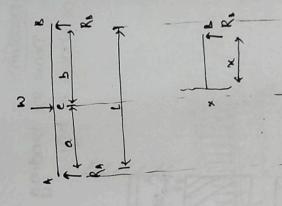
af a, x = 0

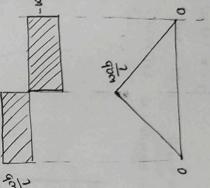
af c, x = a

at c, x = a

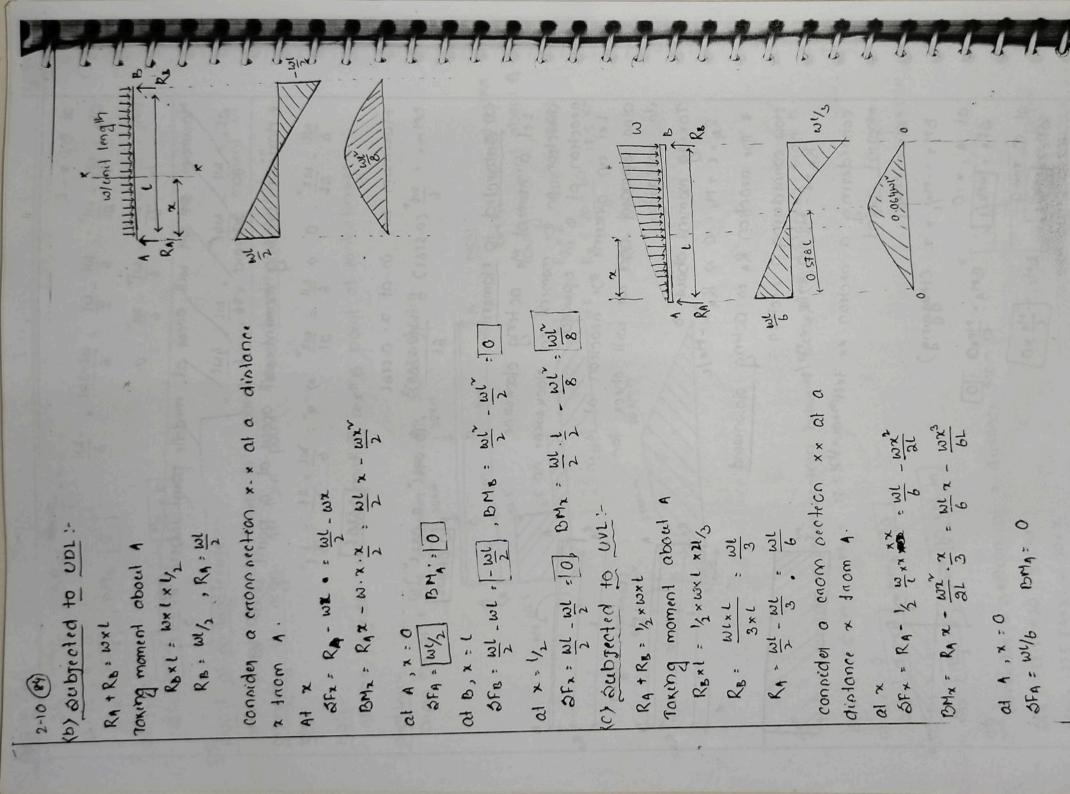
af c, x = a

af c, x = a





× × ×



$$\Delta F_B = \frac{\omega l}{6} - \frac{\omega l^*}{2} + \frac{\omega l}{6} - \frac{\omega l}{2} + \frac{\omega l - 3\omega l}{6} = -\frac{\omega l}{3}$$

$$BM_B = \frac{\omega l^*}{6} - \frac{\omega l^*}{6l} + \frac{\omega l^*}{6} - \frac{\omega l^*}{6} = 0$$

Morament and BM will occur at middle point where
$$x = \frac{2L}{3}$$
 $\Delta F_x = \frac{\omega L}{6} = \frac{\omega L}{6} = \frac{\omega L}{6} = \frac{\omega L}{6}$

* Maximum bending moment will occur at a point where of in zero

$$\frac{Wl}{6} - \frac{\omega x^{\vee}}{2l} = 0 \Rightarrow \frac{Wl}{6} = \frac{\omega x^{\vee}}{2l} \Rightarrow x^{\vee} = \frac{wl}{6} \times \frac{2l}{2l} = \frac{1}{3}l^{\vee}$$

Maximum BM in al x: 0.578L

BM mex =
$$\frac{\omega!}{6}$$
 (0.5781) - $\frac{\omega(0.5781)^3}{61}$ = $(0.0961^2 - 0.0321^2)\omega$ = $0.064\omega t^2$

(d) publiched to Moment:

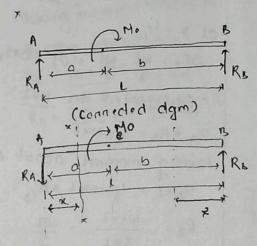
Let a moment Mo acting clackwine direction. An the moment in clockwine no neaction at 15 in apward.

Let up anceme the neaction at A in also appeared and we will object too its validity.

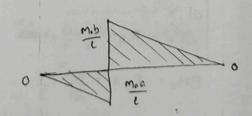
Taking moment about b.

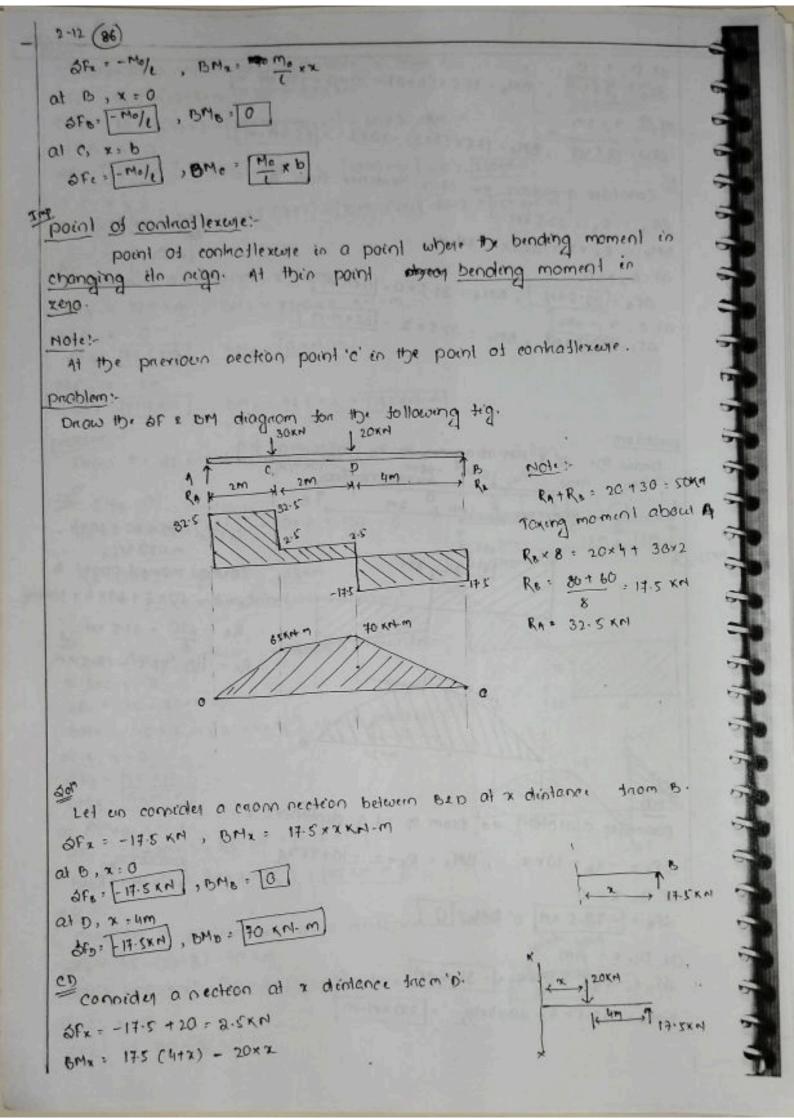
+ The reaction RA in acting downward.

considering a section * tell to the moment point







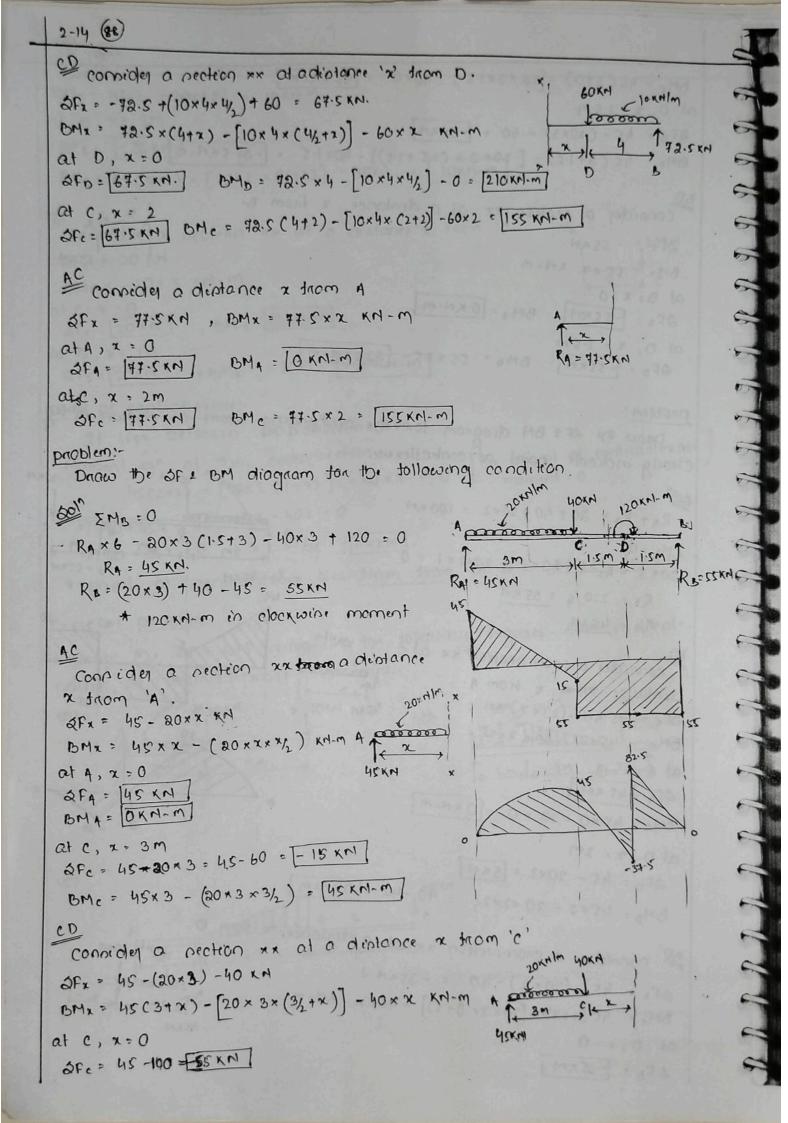


(00 000 00)

- IRE

consider a nection ** from to at a distance 'x'. SFz = - Ro+ 10xx , BMz = Roxx - 10xxx 2/2 al B, x = 0 OF6 : - 72.5 KM , BM6 : 0

at D, z . 4m &FD: -72.5 + 10×4 - 32.5 KM BMD = 72.5× 4- 10×4×4/2 = 210 KM-M



BMc = 45(3+0) - [20 x 3x 1.5] -40 × 0 = [45 KM-M]

PB consider a pection ** at a distance of from B.

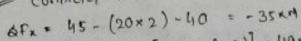


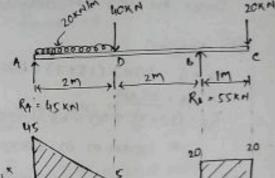
Draw the of 2 BM diagram too the overhanging beam as shown in fig. clearly endicate point of conhallexuse.

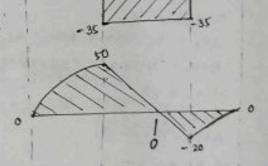
001

confider a compection ** ala dictioner thom x from A.

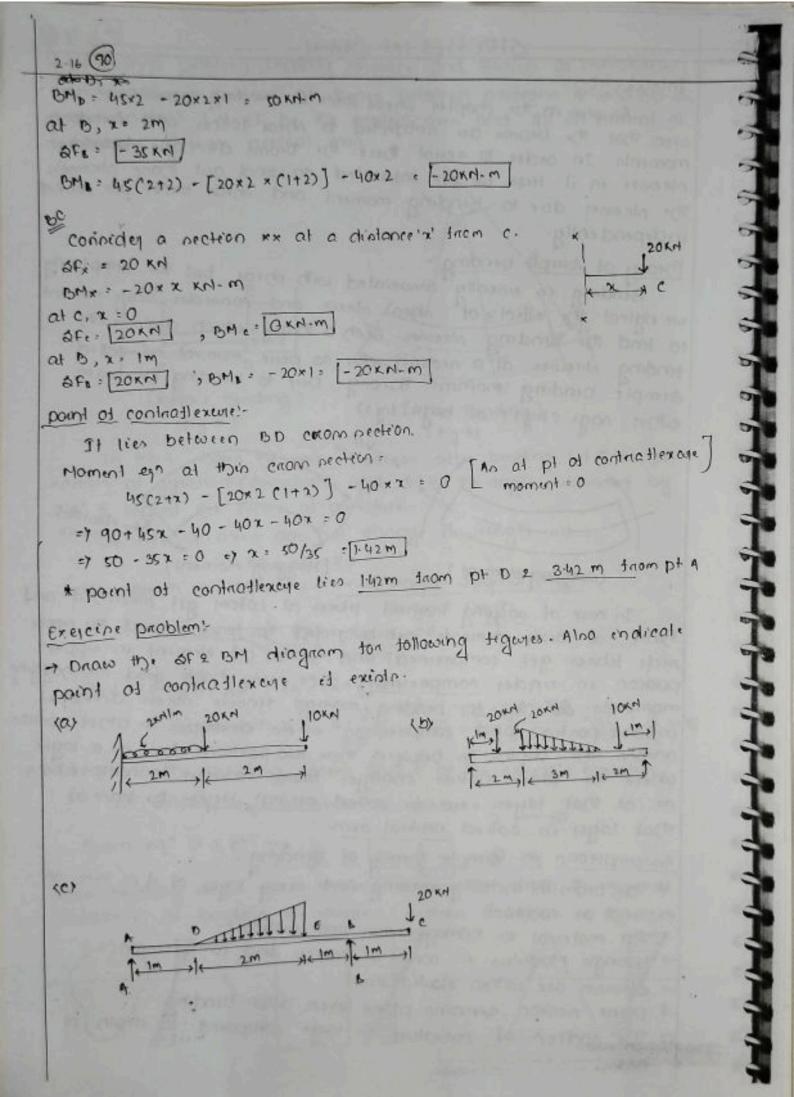
consider a exemptetion ** at a distance a from D.









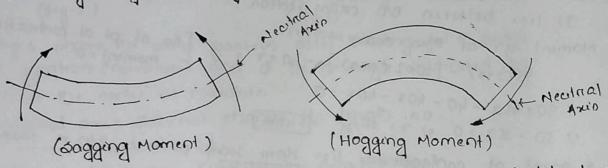


Introduction:

As seen in the chapter shear torce 2 bending moment we had seen that the beams are subjected to shear torces and bending moments. In order to resist these the beams develope broading stresses in it here we are interested to trind out those stresses. The placement due to bending moment and shear torces are tound independently.

Theory of simple bending!

Bending in unually annociated with shear but for simplicity we right the effect of shear street. and consider only moment to tend the bending streets. Such a theory which deals with tending streets at a section due to pure moment in called simple bending moment theory. Due to bending the beam either rags (tigs) or hogs (tigs)



In case of nagging moment tebres at bottom get stretched and bence at lower elements are subjected to tension. and the upper pictor in upper compression. Vice versa bolds good ten hogging moment so due to bending moment tensile stress developes in one portion and compression attended developes in one portion and compression attended developes in other portion across the depth. In between these two portions, there in a layer where the stress nature changes toom tension to compression on at that layer zero is called neutral layer. The trace of that layer in called neutral axis.

Assumptions in simple theory of bending:

The beam in initially almowing and every layer of it in thee to expand on contract

- The material in homogeneous and instrapic.

+ young's Modellus in some en tension and compression.

-> otherner one within elastic limit

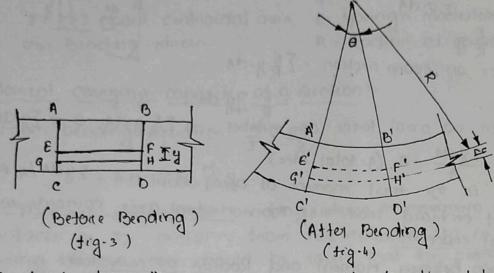
-> prone nection remains plane even after bending.

-> The radius of curvature in large compared to depth of

beam.

Relationship between bending phresses and Radius of curvalenes-

consider a portion of beam between pections at and BD as shown in tigs. Let EF be the neutral axis and QH an element at a distance y from neutral axis.



In tig 4 shows the same position after bending. Let R be the radius of gyration (convolute) and of be the angle subtended by C'of 2 B'D' at the centre of convolute.

The neutral axin does not change its length no

EF = E'F' = R\$

Now, shown in layer GH = Final length - Original length

Original length

But EF = GH = R\$, GH' = (R+4)\$

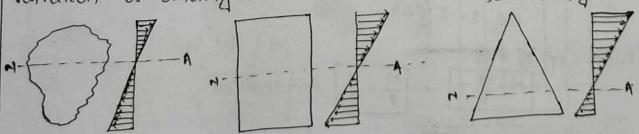
80 Strain = \frac{(R+4)\$\phi\$ - R\$ = \frac{4}{R}\$ - R\$

R\$ = \frac{4}{R}\$ - C

If ob in the bending stress and E be the going's modelus we know $ab : E \times Strain =$ Strain = $\frac{ab}{E}$

From eq 0 2 0 $\frac{\partial b}{\partial t}$, $\frac{d}{dt}$ \Rightarrow $\left[\begin{array}{c} b : \frac{E}{R} \\ \end{array}\right]$ -3

Moraliation of bending ton various nection in shown in try



ととこので

Note:

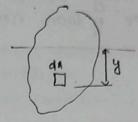
The neutral arein coincides with the example central of the moon-

profilet of be the source on da

Ponce = 0 × dA Total tonce = IndA

But o: Ey

Total tonce on enon nection = ERy-dA



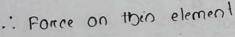
: There in no oxial force on member no ZE y-dA = 0 => Zy-dA=0 i. e Eyida = 0 (A=total Anec)

: EydA in the teast moment of open about N.A. Eycla/A in the distance of centraid from NA. Thun Meutral axis coincide with centraid of channection.

Relationship between Moment and Radius of curvature!

consider an elemental area AA al distance y trom necutral axis in the beam which in shown in tig.

An we know on thin element in given by $ob : \frac{E}{R} y - (from eq.6)$



AF = OBXAA

= E.y. AA

Moment of the resinting torce about neutral axis

AM = AF . Y = E . Y. AA . Y = E Y AA

Total moment on the beam

M = EAM = E E Y DA = E E EY DA

But we know Moment of Inertia (I) of an area in the necond moment of area with nespect to neterence axis

From eg @ 2 6

where,

M: Bending Homent

y = Diotance from needral axub

I = M. I about centracidal axis & young's modules

ob: Bending othern

R : Radiun of remvature

Moment countying capacity of a section!

From bending equation # = ab

05= My

This egr shows that bending stress is maximum at the extreme scurtaces as the distance from neutral axis eys in maximum. as during design care should be taken that the permissible othern (aper) should be less than maximum stress comes)

7: section modulun = Ily

Section Modellen value ton various standard enonnection:

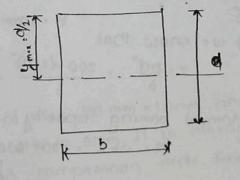
kir Rectangular coon rections

$$J = \frac{b0^{3}}{12}$$

$$\forall \max = \frac{d}{2}$$

$$Z = \frac{J}{4^{mex}} = \frac{b0^{3}/12}{01/2} = \frac{b0^{3}}{6}$$

$$Z = \frac{J}{6^{3}} = \frac{b0^{3}}{6}$$

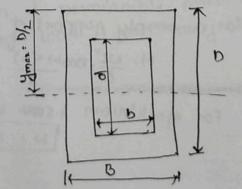


(a) Hollow Rectangular Channection:

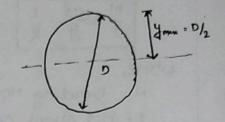
$$J = \frac{150^3}{12} - \frac{60^3}{12} = \frac{150^3 - 60^3}{12}$$

$$y_{\text{max}} = D/2$$
 $z = I/y_{\text{max}} = \frac{Bb^3 - bd^3}{12} / D/2$

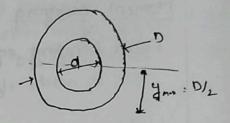
$$z = I/y_{\text{max}} = \frac{Bb^3 - bd^3}{D}$$



(cincular chann pection



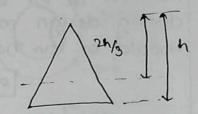
47 Hollow circular Section!



(v) Triangular Chann pection:

$$I : \frac{bh^3}{36}$$

$$\chi = 1/y_{mex} = \frac{bh^3/36}{2h/3} = \frac{bh}{2h}$$



problem:-

A nimply supported beam at upon 6m has a characterist of 200ms

* act mm. It the permissible stress is as NIMM, Find

(a) Maximum intennity at UDL it can commy.

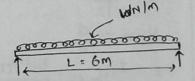
us Maximum concentrated load P acting at the centre

こうさんとうちゅうからからから かっちゅうと

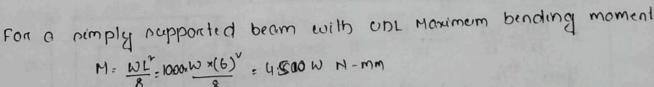
b = 200mm d = 250mm

(a) we know that

$$Z = \frac{bd^{3}}{b} = \frac{200 \times (250)^{3}}{6} = 2083333 \cdot 33 \text{ mm}^{3}$$



Moment contains capacity



For equilibrium 4.500 41666666.67 w = 9259.25 N

(b) Bending moment (H) =
$$\frac{Pab}{L}$$
 = $\frac{P \cdot L \cdot L \cdot L}{L}$
H = $\frac{P \cdot L}{4}$ = $\frac{P \times 6}{4}$ = $1.5 P \cdot M \cdot M$
= 1500 P H · MM

problem !-

A concolor pipe of external diameter 70 mm and thickness 8 mm in used as a simply supported beam over an effective length of 2.5 m. Find the maximum concentrated load that can be applied at 1.5 m from left end of the span it permissible stress in tabe in 150 H1 mm.

External Dia (D): 70mm Internal Dia (d) = 70 - 2x8 = 54mm

$$z = \frac{3}{32} (70^4 - 54^4)$$
= 21748.438 mm³

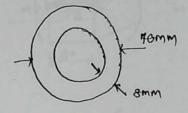
Moment countrying capacity = 150 × 21748.438

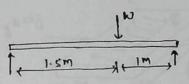
= 3262265. 71 N-mm

Maximum moment developed at the member M' = wab = wx 1500 x 1000 = 600 W H-mm

For equilibrium M'= M 600W = 3262265.71 W = 5437.10 M

A symmetric I-Section bas flanger of size 180 mm x 10mm and its aveilall depth in soomm. Thickness of web in 8mm. It is alreagthend with a plate of size 240 mm x 12mm on compression side. Find the moment of resintance of the pection, if permitable athern in 150 HIMM. How much unitermly distributed load it can come it it in used as a confilered of open 3m.





Let ig be the diplonce of centraid tram the bottom most tibre.

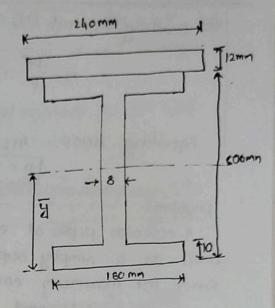
7. Moment of area about bottom tibre

= 240×12×506 + 180×10×495 + 480×48×250 + 180×10×5

240 ×12 + 180 ×10 + 480 ×8 + 180 × 10

= 3397280 = 321.442 mm

それでんとんとなるとと かんかん



Shearing Strendes in Beams:

we had already neen that beamn one nubjected to BM 2 &.F. HOW the relation between a.f & BM one dm = For dx . Now we will onalyse the stresses induced due to shearing torces.

consider a simply supported beam in subjected to an unit throughout the enonnection. For analysis

consider a small element 'olix of the

Here AB = dx.

**

Let Resinting moment al A: M

Resinting moment at B : M+dM

consider a tiber co baring thickness dy at a distance of y tram neutral axin

Bending stars at C-C = My -0 Fonce acting at c-c = My x Anea

lly tonce acting at D-D=

Fonce inbalance between C-D

Total torce acting on appell nede of the champection from N.A.

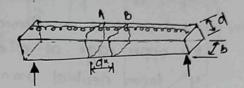
$$F = \int \frac{dH}{dH} y \cdot b \cdot dy = \frac{dH}{I} \int (b \cdot dy) y = \frac{dH}{I} \int dA \cdot y = \frac{dH}{I} (Ay) - 0$$

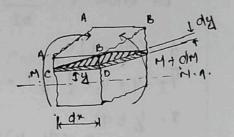
A = Anea Of beam above nectinal axin

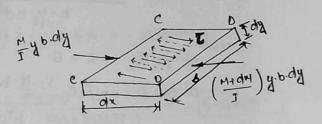
g = Did between C.g of A to N.A.

It is in the intennity of about phrems then the connerponding shear tonce produced on the plane econ :

$$\Rightarrow \frac{dM}{dx} = \frac{rbf}{A\ddot{y}} \Rightarrow Fs = \frac{rbf}{A\ddot{y}} \Rightarrow Fs = \frac{rbf}{A\ddot{y}} \Rightarrow Fs = \frac{FsA\ddot{y}}{bf}$$









As Fs = dm dx

Strong places acrons a tem plandard cross pection;

-> Rectongular section:

connider a rectangular connection baring barib = depth 'd'.

Let up take an element at the appel edge at a distance y' from neutral axin.

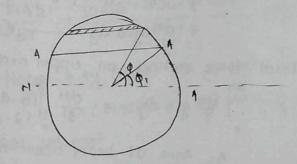
$$T = \frac{1}{2}bd^3$$

Now $E = \frac{F_5 \times (d/2 - 4)b \times \frac{1}{2}(d/2 + 4)}{b \cdot \frac{1}{2}bd^3}$ (porjabolic)

at
$$y = 0$$
, $e = \frac{fs \cdot \cancel{d} \cdot \cancel{b} \cdot \cancel{1} \cdot \cancel{d}}{\cancel{b} \cdot \cancel{d}^{3}} = \frac{6Fs}{4bd} = \frac{1 \cdot S \cdot Fs}{bd} = \frac{1 \cdot S \cdot 9 \cdot 9}{bd}$

-> cincular dection:

consider a section AA ton expirch onea moment at inentic in neguined to tound out M. A. about



Problem :-

A symmetrical T- section in subjected to a special force of 30km Draw the about torce distribution acroom the depth marking values national points.

1+A -

501 Let i be the distance of cg from the top tibre MOW

= (100×12)×6+ (88×12)(44+12) (100×12)+ (88×12) = 29.404mm

M.I about N.A

 $\underline{T} = \frac{100 \times 12^3}{12} + 100 \times 12 \times (29.404 - 6)^7 + \underline{12 \times (88)^3} + (44+12-29.404)^7$ = 2100127.3 mm4

shear staern at Top of flange = 0

- bottom of trange : Anea = 100 x 12 = 1200 mm

(Y1) Distance of cg (Flenge) from N.A = 29.404-6 = 23.404mm

width of flonge(b) = 100 mm

Sheat when (2) Florge Better = FS A 41 = 30×103× 1200×23-404 = [4.01 Almor

- Top of web =

ALLEG (A) - DOC 29 TOK- TE)

wedth at top of web (b) = 12mm

Shear others (2) topweb = FsA &1 = 30×103×1200×23.404 = [33.43 N/mm] bī 12 * 2100127-3

r rectal axis!

Ay abore N.A = Ay of Honge + Ay above NA in web.

= 1200 (29.404-6) + 12x (29.404-12) x 1/2 (29.464-12)

= 29902 · 195 mm3

= 30×103×29902.195 = 35.595 Hlmm abean othern (THA) = FSAY 12 x 2100127.3 bI

- Bottom of web:

problem:

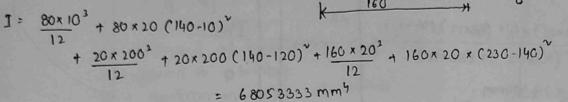
アアアアア

An unsymmetrical I-section as shown in tig subjected to a shear threen of 40KM. Drow the obean others variation diagram.

Distance of neutral axis

80×20 + 200×20 +160×20

= 140 mm



200

20

obean others!

notion of top flange =

$$T = \frac{f_s}{b_1} Ay = \frac{40 \times 1000}{80 \times 68053333} \times 80 \times 20 (140-10) = [1.528 \text{ H/mm}^{\circ}]$$

-> Top of web = (b = 20)

$$T = \frac{F_s}{bI} A y = \frac{40 \times 1000}{20 \times 68053333} \times 80 \times 20 (140 - 10) = 6.113 \times 1 \text{mm}^2$$

- Neutral Axin

$$= \frac{Ay}{80 \times 20} \times (140 - 10) + 20 \times (140 - 20) \times (\frac{140 - 20}{2})$$

$$C_{HA} = \frac{F_s}{b_L} A_{4} = \frac{40 \times 1000}{20 \times 68053333} \times 352000 = 10.345 \text{ N/mm}^{\circ}$$

-> Propo de Bottom at web (b=20)

- Top of Bottom flonge, (b=160)

Till now we had analysed about the beams of name material But in practice there are beams made up of more than one mall. in also tound such beams are called composite beams on Hitched beams. Very common example of this type of beams are tember RING B AL beams with steel plater.

Let un connider

Ere Modelen of elasticity of tember

11, M.J. of timber

Mi: Moment of nexistance of timber

on: Steen in ptimber

71: acction modulum of timber

Ez. Tz, Mz 12, 12: connerponding values for

we know that the moment of merintance MI = OIX XI , H1 : 01 X ZL

total moment of nerintance ton the composite beam M: MI+ML: (01 x X1) + (02 x X2) -0

we also know that at any distance from neutral axis, the strain in both materials will be name

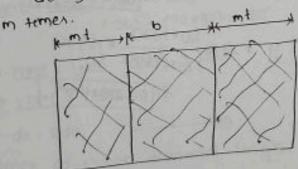
$$\frac{\alpha_1}{\epsilon_1} = \frac{\alpha_1}{\epsilon_2} = \frac{\alpha_1}{\epsilon_1} = \frac{\alpha_1}{\epsilon_2} =$$

m: Ei/E: : Modular natio.

Thus moment of rescalance of element of material -1 in Eiles termes that at element of material-2 placed at name distance from nectual axis we can replace the material 1 by material -2

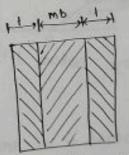
MI = OI XI = M.O. XI [93]

so the width of nection can be neplaced by material - 2 by



Material -1 . Steel Material - 2 : wood

なるとうとうとうとうとうだったい



Material -1 = wood Moterial - 2 = Steel

Here we are conventing one material by analyer. that means we are beinging an equivalent

value of on in terms of or.

problem:

A 200 mm widt and 400 mm deep timber beam in strengthend with 6 mm thick and 200 mm wide ofcel plate as about. Determine the extreme tebre placence, if the pection, in publicled to a moment of 40x11-m take Es/E1 : 20

since Es/E1 = 20

so equivalent tember nection ton 200 mm width of tember

= 20 ×200 = 40000 mm

considering equivalent section

. 16552000 . 159.154mm

1 = 200 × 400 + 200 × 400 (206 - 159.154) + 20 × 200 × 6 (159.154-3)3 = 1.82752 ×10 mm4

Distance of top tibre from N-A = 406-159-154 = 246-846 mm Dinlonce of Junetica from N.A . 159.154 - 6: 153.154mm Bending strent-

at top tibre = My = 40×1000 x 246-846 . [5.403 N/mm]

at the junction (on wood) = Hy . 40×1000 x153.154 = 3.352 HIMM

At the gundton (on steel) = Es My = 20 × 3.352 = 67.04 Mmm

At the bottom tebre = Es My : 20 x 40 x 1000 x 159-159

: 69.670 NImm

50



Inhoduction

Materials used in beams are elastic in nature hence under the action of loads the beam axis deflects. A designer has to decide about beam dimension not only based on strength requirement but also from the consideration of deflection which should be with in prescribed limit.

In mechanical components exconsive deflection may count minolligament and non performance of machine. In buildings excentive detormation gives rine to phychological contest and some temes breaking of flooring, ceiling on nooting materials.

There are various methods at colculating beam deflected in these

-> Double integration / Direct integration / Maculay's method.

-> conjugate beam method

-> costigliono's theorem

Differential Equation tox Deflection:

consider an elemental length AB: ds as shown in tig. Let langento drawn at A 2 B make angles e and etde with x-axis and enterprect il at D and E. Let M be the internection point of these two tongentn-

LEDH : 0, IXEM : 0+de

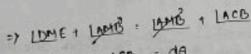
1xEM = 10ME + 8 = 8+08

=> LONE - de

Alno,

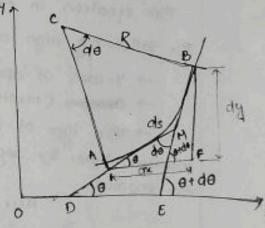
IDME + LAMB = 180"

LAMB+ LACB: 360'- (LCAM+ LCBM) = 360'- (90+90) : 180"



=> LOME = LACE = de

dince do in an elemental length, treating ADF as a triangle,



Distantiating en a wat 'x' we get

$$= \frac{sec^3\theta * \frac{1}{R} * sec^3\theta * \frac{1}{R}}{\frac{1}{R}} * \frac{d^3g | dx^2}{sec^3\theta} * \frac{d^3g | dx^2}{\frac{1}{R}} = \frac{d^3g | dx^2}{sec^3\theta} = \frac{d^3g | dx^2}{(sec^3\theta)^{3/2}} * \frac{d^3g | dx^2}{(1+ton^3\theta)^{3/2}} * \frac{(sec^3\theta * 1+ton^3\theta)^{3/2}}{(1+ton^3\theta)^{3/2}} * \frac{d^3g | dx^2}{\frac{1}{R}} * \frac{d^3$$

In beamn, deflections are small and hince (dylds) in also small. Therefore we can nigled (dy)

Thin equation in collect differential equation of deflection. The tollowing righ conventions are used in dering en 3

-y 4-axis is apposed.

-> Concern Convature in concern towards the yeards.

- This type of convotence occurs on the beam due to nogging moment. Hence the nagging moment in to be considered as the tre moment

Here EI: Hexada Regardity.

Double Integration Hebody

In then method, moment M, at any diplonce & dram one of the perposits in written with the pagging moment as positive. Then from equation

The constants a and a one tound by making one of boundary conditions

(ar at nempty supported notter ends , delection y=0

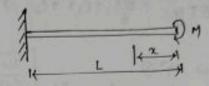
(b) At sexed ends, deflection y:0, dylar:0

(c) At point of symmetry dy/dx . 0

Few different consis-

is contilered publicated to moment at free end:

A contilered beam of length 'L', flexual reigidity ET, subjected to bogging moment at a distance x



al x = L , deflecteon g = 0 = dq = 0

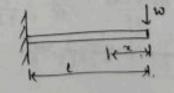
NOW 970

ET dy = -Mx+C1 => 0 = -Mx+C1 => -ML+C1 =0 => C1 = ML

at thee end x=0

(cantilered nubjected to pl load of three end:

know tig



$$AOD \quad ETy = -\frac{\omega x^{1}}{24} + \frac{\omega L^{2}}{6} x - \frac{\omega L^{4}}{8}$$

$$AT = 0 \quad dx = \frac{1}{8} \left(\frac{\omega L^{2}}{6} \right) \cdot \left(\frac{\omega L^{3}}{6ET} \right) \cdot \left(\frac{\omega L^{3}}{6ET} \right)$$

$$AT = \frac{1}{8} \left(\frac{\omega L^{3}}{8} \right) \cdot \left(\frac{\omega L^{3}}{8ET} \right) \cdot \left(\frac{$$

()

ranging than a to we war 13/ 20 perpected - Inci

non try

Mx: 10001 xx = -15xx x 10 xxx =

NXX - MXX

-wzy : - WX3 3 63

120L + C1x + C2 -- WYS 5 + C) x + C2 241 B.M. : R 19

-WL4 +C, => | ET 04 = - 10x4 + C1 => 0 = の。祭。0:兄 מן איר, (a)

=> 0 , -wly +5wly 120 4m1, 120L + WL3 L + C1 3 0 = -WL + WL4 | 120L | 120L | 24 7 ETA : 69,00

30 = - Wx5 + WL3 x 9-HOW ETY

(Slope) WL3 er er अंह at x :0,

(Deglection) - WL4 C1 E1 "

beam acibjected to point load

pepponted Simply

RA: W/2 from Hig,

23/ 7/7 ET SES

1/3

X

₽.

3

125 哥 " WZ" EIB

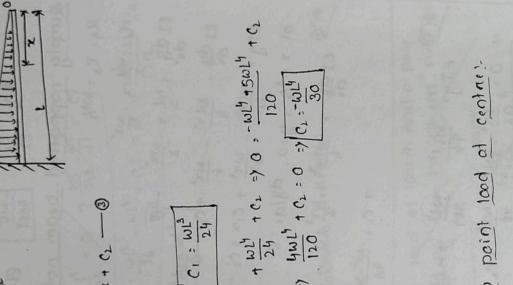
0: 8 at x: 1/2 considering

Now equ @ EI off =

+ (2 =) 0 = WL3-3WL3 48

=> C1 = -21013 32 32 WL x + C, => 0 = WL3 ery ETY : WRS

- WL3 NOW ETY: Wx3 - WL x



We do wit ingh to col: (dellection) (slope) - WL3 -wit 48ES 61 3 3 र्ग र

newbjecked pood Semply responded

- Wx + C1x + C2 - B 6 KZ : We x - wx Mx: WLx - WX wt x RA: RE: WILL

312

到る

2000

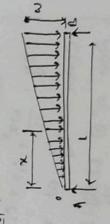
+ (1 => (1 = 148 - 16) w 13 - wt3 - wx3+0, ey 0 = wll = 1 C1 = WIZ-3WIZ 0 = xp/Rp '0= B. en er er er wint ETY : WLX3

אשוא-אוא-אשף => (2=-5/284 WIT 0- 24 (2) + (2 + (2 => 0 = 1 m -17 M 384 6542 will -. 100 met 0

-5 with 2461 EN C3 学等

Simply ruppouled beam publicled to ronging load the sero to w. 341-61 = 101 RAXI: 12 WX LX 1/3 moment about 13 Re: 101 - 16 BuixoL

WZ3 以スト 0 WX TG-EL X 12/2, RA X 海岸 守安 ET



Anoneming deflection of neactions in report of
$$\frac{1}{36}$$
 at $x : 0$, $\frac{1}{3} :$

$$0 = \frac{\omega L^{2}}{12} - \frac{\omega x^{4}}{340} - \frac{\psi \omega L^{3}}{360}$$

$$0 = \frac{60\omega L^{2} - 90\omega x^{4} - 14\omega L^{4}}{7200}$$

$$= 760\omega L^{3}x^{2} - 30\omega x^{4} - 14\omega L^{4} = 0 \quad (All divided by 30\omega)$$

$$= 7x^{4} - 3x^{2}L^{3} - 7/15L^{4} = 0$$

$$x^{2} = 2L^{2} \pm \sqrt{4L^{4} - \frac{4\omega T}{15}L^{4}}$$

$$= 7L^{2}(1 \pm \sqrt{1 - \frac{9}{15}}) = 0.2697L^{2}$$

$$x = 0.5193L$$

How putting value of

al 2: 0.5193 L

ET 9:
$$\frac{\omega \cdot (0.5193L)^3}{36} - \frac{\omega \times (0.5193L)^5}{120L} - \frac{\#\omega l^3}{360} \times (0.5193L)$$

$$= \frac{0.1400 \omega l^4}{36} - \frac{0.0377 L^4 \omega}{120} - \frac{3.635 \omega l^4}{360}$$

proplew !-

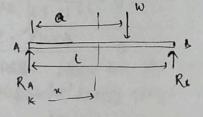
A beam AB of length L in numply supported at the ends and concier a point load 'w' at a distance 'a' snow the left hand, Find ie, Deflection ender the load () Maximum deflecteon

RA + Rs =
$$\omega$$

RA × $L - \omega (l-a) = 0$
 $= \gamma RA = \frac{\omega (l-a)}{L}$

Rs = $\omega - \frac{\omega (l-a)}{L} = \frac{\omega l - \omega l + a\omega}{L} = \omega c$

RA × $\omega = \omega (l-a) = \omega c$
 $= \omega c$



At any point x B.M (M) = - RA x x = - w(l-a) x

ET
$$\frac{dy}{dx} = \frac{-\omega(1-\alpha)}{L} \frac{x^3}{2} + C_1 \frac{-\omega}{2}$$
ET $y = -\frac{\omega(1-\alpha)}{L} \times \frac{x^3}{6} + C_1 \times + C_2 \frac{-\omega}{2}$

$$ETy = \frac{-w(1-a)}{L} \times \frac{L^3}{6} + C_1L = 0 \quad [Aog = 0] \quad [pothing condition]$$

$$\Rightarrow -\frac{\text{Wl}^{2}(1-a)}{6} + \text{Cil} \cdot 0 \Rightarrow \text{Ci} = \frac{\text{Wl}(1-a)}{6}$$
How
$$\text{ETy} = -\frac{\text{W}(1-a)}{1} + \frac{2^{3}}{6} + \frac{\text{Wl}(1-a)}{1} \approx -\frac{1}{2}$$

Maximum deflection !-

For maximum deflection dylax = 0 cslope = 0)

HOW ey's
$$0 = \frac{-\omega(1-\alpha)}{2L} \frac{2^{v} + \omega(1-\alpha)}{6} \frac{2^{v} + \omega(1-\alpha)}{6}$$

= (-4wl*(L-a)

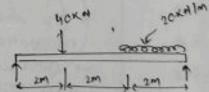
Deflection under the load :-

$$\frac{at}{4} \cdot \frac{1}{6t} \left[\frac{-\omega(t-a)}{L} \frac{b^2 x^3}{6} + \frac{\omega(t-a)}{6} \frac{a}{2} \right] \cdot \frac{1}{6t} \left[\frac{-\omega(t-a)}{6L} \frac{a^3}{6L} + \frac{\omega(t-a)}{6} \frac{a}{6L} \right] \\
= \frac{1}{6t} \left[\frac{\omega(t-a)a}{6} \left[\frac{1-a^3}{6L} \right] \cdot \left[\frac{1}{6t} \frac{\omega(t-a)a}{6L} \left(\frac{1^3-a^3}{6L} \right) \right]$$

problem:

-

Find the maximum deflection and maximum plops ton the bay as phown tig below. Also tend the deflection of a point 3-2 m from A. Take EI = 15 x 10 9 KN/mm

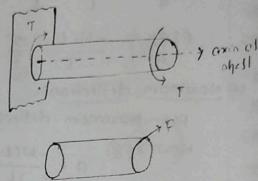


A member is said to be in torsion when it is restricted to restrict to remember about its exist the effect of torsional moment is to true it is spull and bence torriconal moment in called as twinling.

In engineering practice many members are subjected to torsich. 2-shall manomilling pacey from engine to near orde.

-> shall of gearbex

+ Electric motor shall



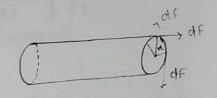
peine tonsion!

こううううううううっていている

5)

A member in haid to be in pere tousion when its caconnection in subjected to only one tousional moment and not accompained by axial forces on bending moment

Now econsider the nection of a shall andle page towns Internal toaces develope in order to counter act thin tornical mement 30 at any element the torce dr developed in in the direction normal to nadial direction.



The force in obvicensly phearing force and then the element in in perse obeat. It da in the orea of the element at distance a licen the axis of notation of shall then,

dF = T x dA (T = shear otress)

dT = dF x R

Appendation of Deougl of Donle Louvicu;

-> The material in homogeneous and instruper.

-> The otherner are withen the elastic limit ite show stress in threatly proportional to obear atrain.

- com rection which are plane before twisting remain plane alter twinting.

-> Radial lines remain radial even atten applying and in tornional moment

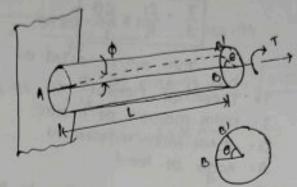
-> The tevent along the shall in uniterm.

Derivation of Towonal Equations

Consider a about of length 't'. Radieur 'R' fixed at one end and oubsected to a torque T at the other end.

Let 'o' be the centre pt of eincular cronn nection on 'B' be a point on number. "AB" in the line on about postellel to the axin of shall.

Dut to application of torque pl B in obitted to B'. It of in the obea nhain (LBOB')



and b' be the angle of twint in length L. then,

RO - BB - LO

It is in the obean niners and is modernes of nigidity then

$$\phi = \frac{\tau_s/q}{q}$$

$$\therefore R\theta \cdot L\phi = L\underline{\tau}_s \qquad [\tau_s : shear place]$$

$$\underline{\tau}_s : \underline{q}\theta \qquad 0$$

demilarly it pl is in considered at any point in between nadical al any dintance 'n' tram centre indead of neutace it can be € = GB - @ [t= shear shear along nodeus]

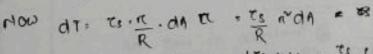
How consider the torrienal resintance developed by on onea 'AA' al dintance in thom centre

It is no the open tours the torce of A4 dF = TdA

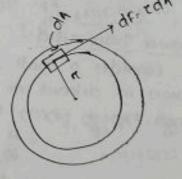
Resisting torraional moment

dT = dF x a = ExdA xa

From eg 1 1 2 1 R: T = T: T.



Total tonque T = Jat . JEgarda = To Jarda = Es J Here Jarda = I (polar moment of Intertra)



R - Diolonce of element from centre

G: Modellen of aigidity

of short

L = Length of about

(i) Hollow circular pedicon with external diameter (D) & internal diameter (

J: 7/32 (D4 - d4) , R: D/2

Zp= J/R = 7/37 (D4-d4) /D/2 = 1/16 D4-d4

power Transmitted:

THE WAY

-

consider a shall subjected to a longere 'T' and notating at 'n' apm. power in deterned as a nate of doing work. Taking second as a unit angle through which torque moves

$$=\frac{N}{60}\times2\pi=\frac{2\pi N}{60}$$

power: work done per necond

= 7 x 2 xr /60

It 'I' in taken an N-m, then unet of power in N-mls i-e walt

Then : 1.3 Then

Then :
$$T = \frac{60P}{2\pi H} = \frac{80 \times 75 \times 10^3}{2 \times 7 \times 200} = \frac{3580.98 \text{ H-m}}{10^2 \times 3580.98 \text{ H-m}}$$
.

We know $\frac{T}{J} = \frac{z}{R} = \frac{7}{R} = \frac{T.R}{z} = \frac{3580.98 \times 10^3}{16} = 51156.94$

$$= \frac{7}{16} = \frac{7}{16} = \frac{7}{16} = \frac{3580.98 \times 10^3}{16} = 51156.94 \Rightarrow d = \frac{3}{16} = 51156.94 \Rightarrow d = \frac{3}{16} = \frac{51156.94 \times 16}{7} = \frac{9}{16} = \frac{3}{16} = \frac{3}{16}$$

0:10 = 7/180 mod

Tm2 80 M NIM" = 80 NIMM" = 80 × 103 NIMM"

 $P = \frac{2\pi NT}{60}$ => $T = \frac{60P}{2\pi N} = \frac{60 \times 736 \times 10^{3}}{2 \times 7 \times 200} = 35141.41 \text{ M-m} = 35141.41 \times 10^{3} \text{ N-mm}$

TOTAL SOR!

$$\frac{T}{J} : \frac{G\Theta}{L} \Rightarrow \Theta : \frac{TL}{GJ} \Rightarrow \frac{35141.41 \times 10^{3} \times 150}{80 \times 10^{3} \times \sqrt{4}} = \frac{67115.14}{d^{3}}$$

=> 67115.14 = 7/180 => d2 = 67115.14 × 180 = 3845 414.79 = d = 156.66 mm

connerponding othern developed:

J: 7/32 dy = 7/32 (156.66) $\frac{T}{J} = \frac{r}{rc} \Rightarrow \frac{35141.41 \times 10^{3}}{59145832.88} = \frac{r}{156.6}$ =59145832.88 mmy 156.66 => T = 46.53 NIMM

AD Emax in 80 Mlmor Extens 60 the about in redic. Torrecord Rigidity / stillners of shotto:

We Know
$$\frac{T}{J}: \frac{GB}{L}$$

$$\Rightarrow T: \frac{GJB}{L} \longrightarrow \mathfrak{D}$$

problem !-

calculate the maximum intensity of shear others enduced and the angle at twist produced on degrees at a solid shatt 120 mm diameter, 12 m long, transmitting 120 xw at 150 apm. Taxe q = 8244/mi

giren data,

Dia of rhatt (d) , 120 mm

length of abett (L) = 12m = 12000mm

Power transmitted (P) = 120 KW = 120 ×103 coall.

9 = 82 KM | mm = 8 2000 M mm

-> Tonque transmitted (T)

$$P = \frac{2\pi NT}{60} = 7 T = \frac{60 \times P}{2\pi N} = \frac{60 \times 120 \times 10^3}{2 \times 7 \times 150} = 7639.43 \text{ N-mm}$$

$$= 7639.43 \times 10^3 \text{ N-mm}$$

→ polon moment of mentic (J) = \(\frac{7}{32}\) d\(^4 = \frac{7}{32} \times (120)\(^4 = 203\)\$ 7520.4 mm\(^4 = \frac{7}{32} \times (120)\(^4 = 203\)\$

- Intensity of obear stress (Cs):

$$\frac{T}{J} = \frac{c_s}{R} \Rightarrow c_s = \frac{T}{J} R = \frac{7639.43 \times 10^3}{20357520.4} \times 60 = 22.51 \text{ Alman}$$

- Angle of twint (0):

of twint (0):
$$\frac{T}{J} = \frac{G\theta}{L} \Rightarrow \theta = \frac{TL}{GJ} = \frac{7639.43 \times 10^{2} \times 12000}{82000 \times 20357520.9} = 0.0549 \text{ mod}$$

$$= 0.0549 \times 180 = 3.14^{\circ}$$

A noted steel short box to transmit 75 yw at 200 rpm. Taxing problem! allowable obean other on ton 1 mm, Find the allowable diameter to the shall it maximum tonque transmitted on each revolution exceeds the mean by 30%.

M = 200 apm C = 70 H1 mm

P = 75 KW = 75000: Wall

problem !-

priore that a hollow shatt is stronger and stilly than the solid shatt of the name material, length and a court weight

bot Let, d = Diameter of solid shat!

di = Deometer of inner nide et hollow matt

dz: Outer diameter of hollow shall

Two shalln have equal weight and length so,

Ts = Resinting tonque of noticed shall Th = Resinting tonque of hollow shall

$$T_{5} = \frac{c}{R_{2}} T_{5} = \frac{c}{d_{2}/2} \pi_{32} (d_{2}^{4} - d_{1}^{4}) = \frac{\pi}{16} \left(\frac{d_{2}^{4} - d_{1}^{4}}{d_{2}} \right) c$$

$$\frac{T_{5}}{T_{5}} = \frac{\pi_{46} (d_{1}^{4} - d_{1}^{4}) \mathcal{E}}{\pi_{16} \mathcal{E} d^{3} d_{2}} = \frac{d_{1}^{4} - d_{1}^{4}}{d^{3} d_{2}} - 0$$

From eg 0 d'= di - di

potting it eg @

$$\frac{T_{5}}{T_{5}} = \frac{d_{5}^{1} - d_{1}^{1}}{d^{2} d_{1} d_{2}} = \frac{d_{2}^{1} - d_{1}^{1}}{(d_{2}^{2} - d_{1}^{2})d_{1}d_{2}} = \frac{(d_{1}^{2} + d_{1}^{2})(d_{2}^{2} - d_{1}^{2})(d_{2}^{2} - d_{1}^{2})}{(d_{1}^{2} - d_{1}^{2})d_{1}d_{2}} = \frac{(d_{1}^{2} + d_{1}^{2})(d_{2}^{2} - d_{1}^{2})}{(d_{1}^{2} - d_{1}^{2})(d_{2} - d_{1}^{2})} = \frac{d_{1}^{2} + d_{1}^{2}}{d_{1} d_{2}}$$

$$= \frac{d_1^{\vee} + d_1^{\vee}}{\sqrt{d_2^{\vee} - d_1^{\vee}} \cdot d_2} = \frac{d_1^{\vee} \left(1 + \left(\frac{d_1}{d_1}\right)^{\vee}\right)}{d_2 \sqrt{1 - \left(\frac{d_1}{d_1}\right)^{\vee}}} = \frac{1 + \left(\frac{d_1}{d_2}\right)^{\vee}}{\sqrt{1 - \left(\frac{d_1}{d_1}\right)^{\vee}}} - 3$$

From the egr 3 we get that numerator in > 1 and denominator (1 no ThyTs

Hollow shatt in stronger than noted shatt

stillness may be detend as the torque required to produce unit

$$\frac{K}{J} = \frac{G \times 1}{1} \Rightarrow K = GJ - 0$$

Ks = Stillness of solid shatt

Ky: atitines of hollow shall

paoblem:

During the test on a numple of steel boy asmm in diameter, it was build that the peril of to KN praduces an extension of 0.095 mm on a length of 200 mm and a torque 200 N-m produces an angellar twent of 0.9° on a length of 250 mm. Find poincion's natio of steel.

d: 25 mm, P: 50 x 103 H, Al: 0.095 mm, L: 200 mm.

A = 7/4 d = 7/4 (25) = 490.87 mm

E = \frac{\sigma}{e} = \frac{P/A}{A1/1} = \frac{PL}{A \Delta 1} = \frac{50 \times 10^3 \times 200}{490.87 \times 0.095} = 214442.02 \text{ Almm'}

T = 200 = N-m = 200 × 103 N-mm , 0: 0.9° = 0.9 × 7 = 0.0157 acd.

L: 250 mm., J= \frac{\pi}{32} d\frac{\gamma}{5} = \frac{\pi}{32} \x(25)\frac{\gamma}{5} = 38349.51 mm\frac{\pi}{32}

 $\frac{T}{J} = \frac{G\theta}{L}$ => $\frac{TL}{F\theta} = \frac{200 \times 10^3 \times 250}{38349.51 \times 0.0157} = 83044.43 \text{ H/mm}^2$

we know the nelation

$$E = 2G(1+4)$$
 => $1+4 = \frac{E}{2G}$ => $4 = \frac{E}{2G}$ =1
$$A = \frac{214442.02}{2 \times 83044.43} - 1 = \boxed{0.291}$$

problem !-

A hollow circular shall of Im length and inner and outer diameters of 45 mm and 125 mm in subjected to a torque of 15 KN-m. If 9 = 80 GP x Determine the maximum shear stress produced and total angle of twint.

501 L = 7m = 7000 mm

d = 75mm, D=125mm

T = 15 KM-m = 15 × 1000 N-m = 15000 × 103 N-mm

9 = 80 (9P= = 80×109 H/mm" = 80×103 H/mm"

7:90

 $J = \frac{\pi}{3} (D^4 - d^4) = \frac{\pi}{32} \left[(125)^4 - (75)^4 \right]$ = 20862138.72 mm4

n n n n n n n n n n n n n n

 $\frac{15000 \times 10^{3}}{20862138.72} = \frac{80 \times 10^{3} \times 0}{7000}$ 20862138-72

=> 0 = 0.06 nad = 3.6°

 $\frac{T}{J} = \frac{z}{R}$ => $\frac{15000 \times 10^3}{20862138 \cdot 37} = \frac{z}{125/2}$ => z = 14.93 NImm

abath aubjected to combined bending & Teointing :

dome times about a subjected to both bending and twinting moment due to its nell weight and notation. Then we have to tend out equivalent binding moment and twisting moment

$$T = \frac{T}{J} R = \frac{T}{\frac{\pi}{32} cl^4} \times \frac{cl}{2} = \frac{16T}{\pi cl^3}$$

then principal sherrer are

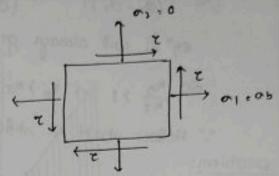
$$O1 = \frac{\sigma_{0}+0}{2} \pm \sqrt{\left(\frac{\sigma_{0}-\sigma}{2}\right)^{v} + v^{v}}$$

$$= \frac{32M}{2 \times \pi d^{3}} \pm \sqrt{\left(\frac{32M}{2 \times \pi d^{3}}\right)^{v} + \left(\frac{16T}{\pi d^{3}}\right)^{v}}$$

$$= \frac{16M}{\pi d^{3}} \pm \sqrt{\left(\frac{16M}{\pi d^{3}}\right)^{v} + \left(\frac{16T}{\pi d^{3}}\right)^{v}}$$

$$= \frac{16}{\pi d^{3}} \left[M \pm \sqrt{M^{v} + 4T^{v}}\right]$$

$$= \frac{32}{\pi d^{3}} \frac{1}{2} \left[M \pm \sqrt{M^{v} + 1^{v}}\right]$$



Mr. = Equivalent benging moment.

months rooms municon

$$t_{\text{mex}} : \sqrt{\left(\frac{\sigma_b - 0}{2}\right)^{\nu} + t^{\nu}}$$

$$= \sqrt{\left(\frac{32M}{7d^3}\right)^{\nu} + \left(\frac{16T}{7d^3}\right)^{\nu}}$$

$$= \frac{16}{7d^3} \sqrt{M^{\nu} + 7^{\nu}}$$

=> Te = VMY17" Te = Equivalent turning moment

$$\frac{\kappa_1}{\kappa_2} = \frac{d_1^4 - d_1^4}{(d_1^2 - d_1^2)^2} = \frac{(d_1^2 + d_1^2)(d_2^2 - d_1^2)}{(d_1^2 - d_1^2)^2} = \frac{d_1^2 + d_1^2}{d_1^2 - d_1^2} - 6$$

eg? 6 will always greater than 1.

: Hollow shatt in stilly than noted shatt

problem !-

A noticed about transmits 250 KW at 100 rpm. It the about stress does not to exceed \$0 alma, what should be the diameter of the shaft? It the shaft in to be replaced by a hollow one whome internal diameter = 0.6 times then outer diometer.

$$T = \frac{60P}{2\pi M} = \frac{60 \times 250 \times 10^3}{2 \times 7 \times 100} = 23873.24 \times 10^3 M \text{-mm}$$

for rollid chatt:

$$\frac{\text{poliol phatt}}{T} = \frac{\tau}{\pi} \Rightarrow T = \frac{\pi}{16} \tau d^2 \Rightarrow d = \sqrt[3]{\frac{16\tau}{\pi\tau}} = \sqrt[3]{\frac{16\times23873\cdot24\times10^5}{\pi\times70}} = \frac{120\cdot20\,\text{mm}}{120\cdot20\,\text{mm}}$$

for hollow shell!

$$\frac{T}{J} = \frac{C}{R} \Rightarrow T = C \times \frac{J}{R} = C \times \frac{T}{16} + \frac{D^4 - d^4}{D} = 70 \times \frac{T}{16} \times \frac{D^4 - (0.6D)^4}{D} = 11.96 D^2$$

en erecored If we well plot a graph by toxing be an the twinking moment no developed in moned on geto twinted shaft enterno of nitrain energy. when I in gradually when Tonger T in applied to anhalf, il gradually endrover. Toursion !-Ahain Energy in · Then angle o alm angle 0

O in x-axin and T in y-axin

Shown Energy (V):

work done

Anea under curre

1/2 TB

1/2 TC IL) = 1/4 TV

T (Tongue)

is strawn energy per unit volume = 2/49

- Hollow obatt

1/2 (10/1)

voleme x 2 (D+d) 400,400,0 10-200 (20+20) 22 x staum energy per enit volume = D,+0, 7 (D1. d4) L

A centerior obath 2m long in neguined to thonnmet 1000 Km. at 300 If the outer diameter of about in 150 mm and inner diameter the maximum obeen othern and street energy Natt. Taxegisc KN/mist 120 mm, Fend paoblem?

```
noblem :-
    At a certain errors section bending moment and terming moment one
reasoned as skn-m and 6kn-m. Find the diameter to design the
                            6 : 20 41 WW
sall it op: 100 nlmm,
pl
 M= 3KN-m = 3000 N-m
 7 = 6 KN- m = 6000 N- m
Equivalant terning moment
                 7 Me = 1/2 [M+ VM+TY]
                         = 1/2 [3+ \3"+6"]
                          = 1/2 [3+ 6.92]
                            = 4.96 KN-M
 Equivalent twinting moment.
                          Te = VM+1"
                             = \( 3^7 + 6^7 \)
                               = 6.92 KN-M
              no design will be done based on Te
    Te yMe
            7e = 6.92 KM-m = 6.92 × 103 × 103 M-mm
                7e = 7/16 td3
             => O = \sqrt[3]{\frac{16 \text{ Te}}{\pi Z}} = \sqrt[3]{\frac{16 \times 6.91 \times 10^6}{\pi \times 50}}
                              = 88.99mm
```

problem:-

A clone coiled bellical spring in made with 12mm diameter wine and in baring mean diameter at 150 mm and 10 complete terms. The modules of reigidity of opening material in 80 KM 1 mm. when a load of 450 KM in applied find - Maximum abear alread

- Strain energy stoned
- -> Deflection produced
- stillness of oping.

geren, P= 1000 KW = 1000×103 Walt, N = 300 Apm. D: 150 mm, d: 120 mm, q: 80 KN/ mm : 80000 H/mm, L: 2000 mm 31830.98 N-m = 31830.98, N-mm $T = \frac{60 \, \text{P}}{270} = \frac{60 \times 1000 \times 10^3}{2000 \times 10^3}$ J= 7/32 (04-04) = 7/32 ((150)4-(120)4) = 29343457:13 mms $C = \frac{T}{J}R = \frac{31830.98 \times 10^3}{29343457 \cdot 13} \times 75' = \frac{81.35 \text{ Alma'}}{29343457 \cdot 13}$ strain energy stored: U= 2"(0"+d") * \ (0"-d") * L $= \frac{(81.35)^{2} (150^{2} + 120^{2})}{4 \times 150^{2} \times 80 \times 1000} \times \frac{1}{4} (150^{2} - 120^{2}) \times 2000$ = 1726131.47 N-mm = 1726.131 N-m = [1726.131 Joule] Close coiled Hellical Spring: The tig. nhown a close coiled bellical spring where, R: Radium of openg w= Axial load, n= Total no of coil. d = Diameter of spring wine. so, Entire length of spring wire = 27Rxn Torrianal moment = F = WR from tornion termula T = T = 7/16 Ed3 => T = 16T = 16WR shown energy in spreng = 2 x volume = (16WR) × 1/4 × 27R1 × 7/4 d

